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Table of Contents

1	Intro	oduction 1				
2	Objects					
	2.1	Basic types				
		2.1.1 Vectors				
		2.1.2 Lists				
		2.1.3 Language objects				
		2.1.3.1 Symbol objects				
		2.1.4 Expression objects				
		2.1.5 Function objects 4				
		2.1.6 NULL				
		2.1.7 Builtin objects and special forms 5				
		2.1.8 Promise objects				
		2.1.9 Dot-dot-dot				
		2.1.10 Environments				
		2.1.11 Pairlist objects				
		2.1.12 The "Any" type				
	2.2	Attributes				
		2.2.1 Names				
		2.2.2 Dimensions				
		2.2.3 Dimnames				
		2.2.4 Classes 7				
		2.2.5 Time series attributes				
	2.3	Special compound objects 8				
		2.3.1 Factors				
		2.3.2 Data frame objects				
3	Eval	uation of expressions 9				
	3.1	Simple evaluation				
	0.1	3.1.1 Constants				
		3.1.2 Symbol lookup				
		3.1.3 Function calls				
		3.1.4 Operators				
	3.2	Control structures				
	J	3.2.1 if				
		3.2.2 Looping				
		3.2.3 repeat				
		3.2.4 while				
		3.2.5 for				
		3.2.6 switch				
	3.3	Elementary arithmetic operations				
	3.3	3.3.1 Recycling rules				

		3.3.2	Propagation of names	. 15	
		3.3.3	Dimensional attributes		
		3.3.4	NA handling	. 15	
	3.4	Indexing	· ·		
		3.4.1	Indexing by vectors		
		3.4.2	Indexing matrices and arrays		
		3.4.3	Indexing other structures		
		3.4.4	Subset assignment		
	3.5		variables		
	0.0	3.5.1	Global environment		
		3.5.2	Lexical environment		
		3.5.3	The call stack		
		3.5.4	Search path		
4	Func	etions		91	
-					
	4.1	_	functions		
		4.1.1	Syntax and examples		
		4.1.2	Arguments		
	4.2		objects		
	4.3	Evaluation	on		
		4.3.1	Evaluation environment		
		4.3.2	Argument matching		
		4.3.3	Argument evaluation	23	
		4.3.4	Scope	. 24	
	4.4	Closures		. 25	
5	Object-oriented programming 2				
	5.1	Definition	n	26	
	5.2		nce		
	5.3		dispatching		
	5.4		od		
	5.5		hod		
	5.6		nethods		
	5.7	-	methods		
6	Com	nuting	on the language	32	
-	6.1		anipulation of language objects		
	0.1		animitation of fanguage objects	ഉമ	
	6.2	Substitut	tions	. 34	
	6.2 6.3	Substitut More on	tions	. 34	
	6.2 6.3 6.4	Substitut More on Evaluation	tions	. 34 . 35 . 36	
	6.2 6.3 6.4 6.5	Substitut More on Evaluation Manipula	tions	34353637	
	6.2 6.3 6.4	Substitut More on Evaluation Manipula	tions	34353637	
7	6.2 6.3 6.4 6.5 6.6	Substitut More on Evaluatio Manipula Manipula	tions	. 34 . 35 . 36 . 37 . 39	
7	6.2 6.3 6.4 6.5 6.6	Substitut More on Evaluatio Manipula Manipula	tions	. 34 . 35 . 36 . 37 . 39	
7	6.2 6.3 6.4 6.5 6.6 Syst	Substitut More on Evaluatio Manipula Manipula em and Operatin	tions evaluation on of expression objects ation of function calls ation of functions d foreign language interfaces	34 35 36 37 39 40	

8 Exception handling			42				
	8.1	stop		42			
	8.2	-					
	8.3	on.exit		. 42			
	8.4	$\operatorname{restart}$		42			
	8.5	Error opt	ions	. 43			
9	Debu	bebugging 44					
	9.1	browser.		44			
	9.2	debug/ur	debug	. 45			
	9.3	trace/unt	race	. 45			
	9.4	traceback		46			
10 Parser				47			
	10.1	The par	sing process	. 47			
		10.1.1	Modes of parsing				
		10.1.2	Internal representation				
		10.1.3	Deparsing				
	10.2	Tokens.		. 48			
		10.2.1	Constants	48			
		10.2.2	Identifiers	49			
		10.2.3	Reserved words	49			
		10.2.4	Special operators	. 49			
		10.2.5	Separators	. 49			
		10.2.6	Operator tokens	50			
		10.2.7	Grouping symbols	. 50			
		10.2.8	Indexing tokens	. 50			
	10.3	Expressi	ons	50			
		10.3.1	Function calls	. 50			
		10.3.2	Infix and prefix operators	. 51			
		10.3.3	Index constructions	52			
		10.3.4	Compound expressions				
		10.3.5	Flow control elements	52			
		10.3.6	Function definitions	53			
Fu	nctio	and V	Variable Index	54			
Δn	nend	iv Δ	References	56			

1 Introduction

R is a system for statistical computation and graphics. It provides, among other things, a programming language, high level graphics, interfaces to other languages and debugging facilities. This manual details and defines the R language.

The R language is a dialect of S which was designed in the 1980s and has been in widespread use in the statistical community since. Its principal designer, John M. Chambers, was awarded the 1998 ACM Software Systems Award for S.

The language syntax has a superficial similarity with C, but the semantics are of the FPL (functional programming language) variety with stronger affinities with Lisp and APL. In particular, it allows "computing on the language", which in turn makes it possible to write functions that take expressions as input, something that is often useful for statistical modeling and graphics.

It is possible to get quite far using R interactively, executing simple expressions from the command line. Some users may never need to go beyond that level, others will want to write their own functions either in an ad hoc fashion to systematize repetitive work or with the perspective of writing add-on packages for new functionality.

The purpose of this manual is to document the language *per se*. That is, the objects that it works on, and the details of the expression evaluation process, which are useful to know when programming R functions. Major subsystems for specific tasks, such as graphics, are only briefly described in this manual and will be documented separately.

Although much of the text will equally apply to S, there are also some substantial differences, and in order not to confuse the issue we shall concentrate on describing R.

The design of the language contains a number of fine points and common pitfalls which may surprise the user. Most of these are due to consistency considerations at a deeper level, as we shall explain. There are also a number of useful shortcuts and idioms, which allow the user to express quite complicated operations succinctly. Many of these become natural once one is familiar with the underlying concepts. In some cases, there are multiple ways of performing a task, but some of the techniques will rely on the language implementation, and others work at a higher level of abstraction. In such cases we shall indicate the preferred usage.

Some familiarity with R is assumed. This is not an introduction to R but rather a programmers' reference manual. Other manuals provide complementary information: in particular section "Preface" in R Introduction provides an introduction to R and section "System and foreign language interfaces" in Writing R Extensions details how to extend R using compiled code.

2 Objects

In every computer language variables (or symbols) provide a means of accessing the data stored in memory. R does not provide direct access to the computer's memory but rather provides a number of specialized data structures we will refer to as objects. These objects are referred to through symbols or variables. In R, however, the symbols are themselves objects and can be manipulated in the same way as any other object. This is different from many other languages and has wide ranging effects.

In this chapter we provide preliminary descriptions of the various data structures provided in R. More detailed discussions of many of them will be found in the subsequent chapters. The R specific function typeof returns the type of an R object. Note that in the C code underlying R, all objects are pointers to a structure with typedef SEXPREC; the different R data types are represented in C by SEXPTYPE, which determines how the information in the various parts of the structure is used.

The following table describes the possible values returned by typeof and what they are.

```
NULL
                    Null
symbol
                    a variable name
pairlist
                    a pairlist object
closure
                    a function
environment
                    an environment
                    an object used to implement lazy evaluation
promise
language
                    an R language construct
                    a builtin function that does not evaluate its arguments
special
builtin
                    a builtin function that evaluates its arguments
                    a vector containing logical values
logical
                    a vector containing integer values
integer
double
                    a vector containing real values
                    a vector containing complex values
complex
character
                    a vector containing character values
                    the special variable length argument ***
                    a special type that matches all types ***
any
expression
                    an expression object
list
                    a list
                    an external pointer object
externalptr
```

I don't think that the user can get a hold of items marked with a '***'; at least not easily; counter examples would be appreciated.

Function mode gives information about the *mode* of an object in the sense of Becker, Chambers & Wilks (1988), and is fully compatible with other implementations of the S language. Finally, the function storage.mode returns the *storage mode* of its argument in the sense of Becker et al. (1988). It is generally used when calling functions written in another language, such as C or FORTRAN, to ensure that R objects have the data type expected by the routine being called. (In the S language, vectors with integer or real values are both of mode "numeric", so their storage modes need to be distinguished.)

```
> x <- 1:3
> typeof(x)
[1] "integer"
> mode(x)
```

```
[1] "numeric"
> storage.mode(x)
[1] "integer"
```

R objects are often coerced to different types during computations. There are also many functions available to perform explicit coercion. When programming in the R language the type of an object generally doesn't affect the computations, however, when dealing with foreign languages or the operating system it is often necessary to ensure that an object is of the correct type.

2.1 Basic types

2.1.1 Vectors

Vectors can be thought of as contiguous cells containing homogeneous data. Cells are accessed through indexing operations such as x[5]. More details are given in Section 3.4 [Indexing], page 16.

R has five basic vector types: logical, integer, real, complex, and string (or character). The modes and storage modes for the different vector types are listed in the following table.

type of	mode	storage.mode
logical	logical	logical
integer	numeric	integer
double	numeric	double
complex	complex	complex
character	character	character

Single numbers, such as 4.2, and strings, such as "four point two" are still vectors, of length 1; there are no more basic types. Vectors with length zero are possible (and useful).

String vectors have mode and storage mode "character", which is somewhat confusing.

2.1.2 Lists

Lists ("generic vectors") are another kind of data storage. Lists have elements, each of which can contain any type of R object, i.e. the elements of a list do not have to be of the same type. List elements are accessed through three different indexing operations. These are explained in detail in Section 3.4 [Indexing], page 16.

2.1.3 Language objects

There are three types of objects that constitute the R language. They are *calls*, *expressions*, and *names*. Since R has objects of type "expression" we will try to avoid the use of the word expression in other contexts. In particular syntactically correct expressions will be referred to as *statements*.

These objects have modes "call", "expression", and "name", respectively.

They can be created directly from expressions using the quote mechanism and converted to and from lists by the as.list and as.call functions. Components of the parse tree can be extracted using the standard indexing operations.

2.1.3.1 Symbol objects

Symbols refer to R objects. The name of any R object is usually a symbol. Symbols can be created through the function quote.

Symbol have mode "name", storage mode "symbol", and type "symbol". They can be coerced to and from character strings using as.character and as.name. They naturally appear as atoms of parsed expressions, try e.g. as.list(quote(x + y)).

2.1.4 Expression objects

In R one can have objects of type "expression". An expression contains one or more statements. A statement is a syntactically correct collection of symbols. Expression objects are similar to language objects in that they contain parsed, but unevaluated R statements. The main difference is that an expression object can contain several such expressions. Another more subtle difference is that objects of type "expression" are only evaluated when explicitly passed to eval, whereas language objects may get evaluated in some unexpected cases.

An expression object behaves much like a list and its components should be accessed in the same way as the components of a list.

2.1.5 Function objects

In R functions are objects and can be manipulated in much the same way as any other object. Functions (or more precisely, function closures) have three basic components, a formal argument list, a body and an environment. The argument list is a comma-separated list of arguments. An argument can be a symbol, or a 'symbol = default' construct, or the special argument '...'. The second form of argument is used to specify a default value for an argument. This value will be used if the function is called without any value specified for that argument. The '...' argument is special and can contain any number of arguments. It is generally used if the number of arguments is unknown or in cases where the arguments will be passed on to another function.

The body is a parsed R statement. It is usually a collection of statements in braces but it can be a single statement, a symbol or even a constant.

A function's environment is the environment that was active at the time that the function was created. Any symbols bound in that environment are *captured* and available to the function. This combination of the code of the function and the bindings in its environment is called a 'function closure', a term from functional programming theory. In this document we generally use the term 'function', but use 'closure' to emphasize the importance of the attached environment.

It is possible to extract and manipulate the three parts of a closure object using formals, body, and environment constructs (all three can also be used on the left hand side of assignments). The last of these can be used to remove unwanted environment capture.

There is also a facility for converting functions to and from list structures using as.list and as.function. These have been included to provide compatibility with S and their use is discouraged.

2.1.6 NULL

There is a special object called NULL. It is used whenever there is a need to indicate or specify that an object is absent. It should not be confused with a vector or list of zero length.

The NULL object has no type and no modifiable properties. There is only one NULL object in R, to which all instances refer. To test for NULL use is.null. You cannot set attributes on NULL.

2.1.7 Builtin objects and special forms

These two kinds of object contain the built-in functions of R, i.e., those that are displayed as .Primitive in code listings. The difference between the two lies in the argument handling. Builtin functions have all their arguments evaluated and passed to the primitive function, in accordance with *call-by-value*, whereas special functions pass the unevaluated expressions to the internal function.

From the R language, these objects are just another kind of function, except that their definition cannot be listed. The typeof function can distinguish them from interpreted functions.

2.1.8 Promise objects

Promise objects are part of R's lazy evaluation mechanism. They contain three slots, a value, an expression, and an environment. When a function is called the arguments are matched and then each of the formal arguments is bound to a promise. The expression that was given for that formal argument and a pointer to the environment the function was called from are stored in the promise.

Until that argument is accessed there is no *value* associated with the promise. When the argument is accessed, the stored expression is evaluated in the stored environment, and the result is returned. The result is also saved by the promise. This allows the programmer to access either the value or the expression associated with the promise.

Within the R language, promise objects are almost only seen implicitly. Actual function arguments are of this type (which is the whole point of lazy evaluation). substitute will extract the content of the expression slot, and there is a delay function that will make a promise out of an expression. There is no fail-safe way of checking whether an object is a promise or not.

2.1.9 Dot-dot-dot

The '...' object type is stored as a type of list. The components of '...' can be accessed in the usual list manner from C code, but is not easily accessed as an object in interpreted code. The object can be captured as a list, so for example in table one sees

```
args <- list(...)
## ....
for (a in args) {
## ....</pre>
```

If a function has '...' as a formal argument then any actual arguments that do not match a formal argument are matched with '...'.

2.1.10 Environments

Environments can be thought of as consisting of two things. A *frame*, or set of symbol-value pairs and a pointer to an enclosing environment. When a value is sought for a symbol the frame is examined and if a matching symbol is found it will be returned. If not the enclosing environment is then accessed and the process repeated. Environments form a tree structure in which an environment can have multiple children, but only one parent.

Environments are created implicitly by function calls, but may also be created directly by new.env. The frame content of an environment can be accesses and manipulated by use of get and assign as well as eval and evalq.

There is currently no way directly to access the enclosure of a given environment.

Notice that environments unlike any other R object cannot be copied. Thus, if you assign several symbols the same environment and change one, the others will change too. In particular, assigning attributes to an environment can lead to surprises.

2.1.11 Pairlist objects

Pairlist objects are similar to Lisp's dotted-pair lists. They are used extensively in the internals of R, but are rarely visible in interpreted code, although they are returned by formals, and can be created by (e.g.) the pairlist function. A zero-length pairlist is NULL, as would be expected in Lisp but in contrast to a zero-length list. Each such object has three slots, a CAR value, a CDR value and a TAG value. The TAG value is a text string and CAR and CDR usually represent, respectively, a list item (head) and the remainder (tail) of the list with a NULL object as terminator (the CAR/CDR terminology is traditional Lisp and originally referred to the address and decrement registers on an early 60's IBM computer).

Pairlists are handled in the R language in exactly the same way as generic vectors ("lists"). In particular, elements are accessed using the same [[]] syntax. The use of pairlists is deprecated since generic vectors are usually more efficient to use. When an internal pairlist is accessed from R it is generally converted to and from a generic vector.

2.1.12 The "Any" type

It is not really possible for an object to be of "Any" type, but it is nevertheless a valid type value. It gets used in certain (rather rare) circumstances, e.g. as.vector(x, "any"), indicating that type coercion should not be done.

2.2 Attributes

All objects except NULL can have one or more attributes attached to them. Attributes are stored as a list where all elements are named. The list of attributes can be obtained using attributes and set by attributes<-, individual components are accessed using attr and attr<-.

Some attributes have special accessor functions (e.g. levels<- for factors) and these should be used when available. In addition to hiding details of implementation they may perform additional operations. R attempts to intercept calls to attr<- and to attributes<- that involve the special attributes and to enforce the consistency checks.

Matrices and arrays are simply vectors with the attribute dim and optionally dimnames attached to the vector.

Attributes are used to implement the class structure used in R. If an object has a class attribute then that attribute will be examined during evaluation. The class structure in R is described in detail in Chapter 5 [Object-oriented programming], page 26.

2.2.1 Names

A names attribute, when present, labels the individual elements of a vector or list. When an object is printed the names attribute, when present, is used to label the elements. The names attribute can also be used for indexing purposes, for example, quantile(x)["25%"].

One may get and set the names using names and names<- constructions. The latter will perform the necessary consistency checks to ensure that the names attribute has the proper type and length.

Pairlists and one-dimensional arrays are treated specially. For pairlist objects, a virtual names attribute is used; the names attribute is really constructed from the tags of the list components. For one-dimensional arrays the names attribute really accesses dimnames[[1]].

2.2.2 Dimensions

The dim attribute is used to implement arrays. The content of the array is stored in a vector in column-major order and the dim attribute is a vector of integers specifying the respective extents of the array. R ensures that the length of the vector is the product of the lengths of the dimensions. The length of one or more dimensions may be zero.

A vector is not the same as a one-dimensional array since the latter has a dim attribute of length one, whereas the former has no dim attribute.

2.2.3 Dimnames

Arrays may name each dimension separately using the dimnames attribute which is a list of character vectors. The dimnames list may itself have names which are then used for extent headings when printing arrays.

2.2.4 Classes

R has an elaborate class system, controlled via the class attribute. This attribute is a character vector containing the list of classes that an object inherits from. This forms the basis of the "generic methods" functionality in R.

This attribute can be accessed and manipulated virtually without restriction by users. There is no checking that an object actually contains the components that class methods expect. Thus, altering the **class** attribute should be done with caution, and when they are available specific creation and coercion functions should be preferred.

2.2.5 Time series attributes

The tsp attribute is used to hold parameters of time series, start, end, and frequency. This construction is mainly used to handle series with periodic substructure such as monthly or quarterly data.

2.3 Special compound objects

2.3.1 Factors

Factors are used to describe items that can have a finite number of values (gender, social class, etc.). A factor has a levels attribute and class "factor". Optionally, it may also contain a contrasts attribute which controls the parametrisation used when the factor is used in a modeling functions.

A factor may be purely nominal or may have ordered categories. In the latter case, it should be defined as such and have a class vector c("ordered", "factor").

Factors are currently implemented using an integer array to specify the actual levels and a second array of names that are mapped to the integers. Rather unfortunately users often make use of the implementation in order to make some calculations easier. This, however, is an implementation issue and is not guaranteed to hold in all implementations of R.

2.3.2 Data frame objects

Data frames are the R structures which most closely mimic the SAS or SPSS data set, i.e. a "cases by variables" matrix of data.

A data frame is a list of vectors, factors, and/or matrices all having the same length (number of rows in the case of matrices). In addition, a data frame generally has a names attribute labeling the variables and a row.names attribute for labeling the cases.

A data frame can contain a list that is the same length as the other components. The list can contain elements of differing lengths thereby providing a data structure for ragged arrays. However, as of this writing such arrays are not generally handled correctly.

3 Evaluation of expressions

When a user types a command at the prompt (or when an expression is read from a file) the first thing that happens to it is that the command is transformed by the parser into an internal representation. The evaluator executes parsed R expressions and returns the value of the expression. All expressions have a value. This is the core of the language.

This chapter describes the basic mechanisms of the evaluator, but avoids discussion of specific functions or groups of functions which are described in separate chapters later on or where the help pages should be sufficient documentation.

Users can construct expressions and invoke the evaluator on them.

3.1 Simple evaluation

3.1.1 Constants

Any number typed directly at the prompt is a constant and is evaluated.

> 1 [1] 1

Constants are fairly boring and to do more we need symbols.

3.1.2 Symbol lookup

When a new variable is created it must have a name so it can be referenced and it usually has a value. The name itself is a symbol. When a symbol is evaluated its value is returned. Later we shall explain in detail how to determine the value associated with a symbol.

In this small example y is a symbol and its value is 4. A symbol is an R object too, but one rarely needs to deal with symbols directly, except when doing "programming on the language" (Chapter 6 [Computing on the language], page 32).

> y <- 4 > y [1] 4

3.1.3 Function calls

Most of the computations carried out in R involve the evaluation of functions. We will also refer to this as function *invocation*. Functions are invoked by name with a list of arguments separated by commas.

```
> mean(1:10)
[1] 5.5
```

In this example the function mean was called with one argument, the vector of integers from 1 to 10.

R contains a huge number of functions with different purposes. Most are used for producing a result which is an R object, but others are used for their side effects, e.g., printing and plotting functions.

Function calls can have tagged arguments, as in plot(x, y, pch = 3) arguments without tags are known as positional since the function must distinguish their meaning from their sequential positions among the arguments of the call, e.g., that x denotes the abscissa variable and y the ordinate. The use of tags is an obvious convenience for functions with a large number of optional arguments.

A special type of function calls can appear on the left hand side of the assignment operator as in

```
> class(x) <- "foo"
```

What this construction really does is to call the function class<- with the original object and the right hand side. This function performs the modification of the object and returns the result which is then stored back into the original variable. (At least conceptually, this is what happens. Some additional effort is made to avoid unnecessary data duplication.)

3.1.4 Operators

R allows the use of arithmetic expressions using operators similar to those of the C programming language, for instance

```
> 1 + 2
[1] 3
```

Expressions can be grouped using parentheses, mixed with function calls, and assigned to variables in a straightforward manner

```
> y <- 2 * (a + log(x))
```

R contains a number of operators. They are listed in the table below.

```
- Minus, can be unary or binary
```

+ Plus, can be unary or binary

! Unary not

Tilde, used for formulae, can be either unary or binary

? Help

: Sequence, binary

* Multiplication, binary

/ Division, binary

[^] Exponentiation, binary

%x% Special binary operators, x can be replaced by anything

Modulus, binaryLess than, binary

> Greater than, binary

== Equal to, binary

>= Greater than or equal to, binary
<= Less than or equal to, binary

& And, binary, vectorized

&& And, binary, not vectorized

Or, binary, vectorized
Or, binary, not vectorized

<- Left assignment, binary

Left assignment, binary, shouldn't be used

-> Right assignment, binary

\$ List subset, binary

Except for the syntax, there is no difference between applying an operator and calling a function. In fact, x + y can equivalently be written "+"(x, y). Notice that since '+' is a non-standard function name, it needs to be quoted.

R deals with entire vectors of data at a time, and most of the elementary operators and basic mathematical functions like log are vectorized (as indicated in the table above). This means that e.g. adding two vectors of the same length will create a vector containing the element-wise sums, implicitly looping over the vector index. This applies also to other operators like -, *, and / as well as to higher dimensional structures. Notice in particular that multiplying two matrices does not produce the usual matrix product (the %*% operator exists for that purpose). Some finer points relating to vectorized operations will be discussed in Section 3.3 [Elementary arithmetic operations], page 15.

To access individual elements of a vector, one generally uses the x[i] construction.

```
> x <- rnorm(5)
> x
[1] -0.12526937 -0.27961154 -1.03718717 -0.08156527 1.37167090
> x[2]
[1] -0.2796115
```

List components are more commonly accessed using x\$a or x[[i]].

```
> x <- options()
> x$prompt
[1] "> "
```

Indexing constructs can also appear on the right hand side of an assignment.

Like the other operators, indexing is really done by functions, and one could have used "["(x, 2) instead of x[2].

R's indexing operations contain many advanced features which are further described in Section 3.4 [Indexing], page 16.

3.2 Control structures

Computation in R consists of sequentially evaluating *statements*. Statements, such as x<-1:10 or mean(y), can be separated by either a semi-colon or a new line. Whenever the evaluator is presented with a syntactically complete statement that statement is evaluated and the *value* returned. The result of evaluating a statement can be referred to as the value of the statement¹ The value can always be assigned to a symbol.

Both semicolons and new lines can be used to separate statements. A semicolon always indicates the end of a statement while a new line *may* indicate the end of a statement. If the current statement is not syntactically complete new lines are simply ignored by the evaluator. If the session is interactive the prompt changes from '>' to '+'.

```
> x <- 0; x + 5
[1] 5
> y <- 1:10
> 1; 2
```

Evaluation always takes place in an environment. See Section 3.5 [Scope of variables], page 18 for more details.

[1] 1 [1] 2

Statements can be grouped together using braces '{' and '}'. A group of statements is sometimes called a *block*. Single statements are evaluated when a new line is typed at the end of the syntactically complete statement. Blocks are not evaluated until a new line is entered after the closing brace. In the remainder of this section, *statement* refers to either a single statement or a block.

```
> { x <- 0
+ x + 5
+ }
[1] 5</pre>
```

3.2.1 if

The if/else statement conditionally evaluates two statements. There is a *condition* which is evaluated and if the *value* is TRUE then the first statement is evaluated; otherwise the second statement will be evaluated. The if/else statement returns, as its value, the value of the statement that was selected. The formal syntax is

```
if ( statement1 )
    statement2
else
    statement3
```

First, statement1 is evaluated to yield value1. If value1 is a logical vector with first element TRUE then statement2 is evaluated. If the first element of value1 is FALSE then statement3 is evaluated. If value1 is a numeric vector then statement3 is evaluated when the first element of value1 is zero and otherwise statement2 is evaluated. Only the first element of value1 is used. All other elements are ignored. If value1 has any type other than a logical or a numeric vector an error is signalled.

If/else statements can be used to avoid numeric problems such as taking the logarithm of a negative number. Because if/else statements are the same as other statements you can assign the value of them. The two examples below are equivalent.

```
> if( any(x) <= 0 ) y <- log(1+x) else y <- log(x) > y <- if( any(x)<= 0 ) log(1+x) else log(x)
```

The else clause is optional. The statement if $(any(x) \le 0) x \le x[x \le 0]$ is valid. When the if statement is not in a block the else, if present, must appear on the same line as statement1. Otherwise the new line at the end of statement1 yields a syntactically complete statement that is evaluated.

If/else statements can be nested.

```
if ( statement1 )
    statement2
else if ( statement3 )
    statement4
else if ( statement5 )
    statement6
else
    statement8
```

One of the even numbered statements will be evaluated and the resulting value returned. If the optional else clause is omitted and all the odd numbered *statement*'s evaluate to FALSE no statement will be evaluated and NULL is returned.

The odd numbered *statements* are evaluated, in order, until one evaluates to TRUE and then the associated even numbered *statement* is evaluated. In this example, *statement6* will only be evaluated if *statement1* is FALSE and *statement3* is FALSE and *statement5* is TRUE. There is no limit to the number of else if clauses that are permitted.

3.2.2 Looping

R has three statements that provide explicit looping.² They are for, while and repeat. The two builtin constructs, next and break, provide additional control over the evaluation. Each of the three statements returns the value of the last statement that was evaluated. It is possible, although uncommon, to assign the result of one of these statements to a symbol. R provides other functions for implicit looping such as tapply, apply, and lapply. In addition many operations, especially arithmetic ones, are vectorized so you may not need to use a loop.

There are two statements that can be used to explicitly control looping. They are break and next. The break statement causes an exit from the innermost loop that is currently being executed. The next statement immediately causes control to return to the start of the loop. The next iteration of the loop (if there is one) is then executed. No statement below next in the current loop is evaluated.

3.2.3 repeat

The repeat statement causes repeated evaluation of the body until a break is specifically requested. This means that you need to be careful when using repeat because of the danger of an infinite loop. The syntax of the repeat loop is

```
repeat statement
```

When using repeat, statement must be a block statement. You need to both perform some computation and test whether or not to break from the loop and usually this requires two statements.

3.2.4 while

The while statement is very similar to the repeat statement. The syntax of the while loop is

```
while ( statement1 ) statement2
```

where statement1 is evaluated and if its value is TRUE then statement2 is evaluated. This process continues until statement1 evaluates to FALSE. If statement2 is never evaluated then while returns NULL and otherwise it returns the value of the last evaluation of statement2.

² Looping is the repeated evaluation of a statement or block of statements.

3.2.5 for

```
The syntax of the for loop is for ( name in vector ) statement1
```

where vector can be either a vector or a list. For each element in vector the variable name is set to the value of that element and statement1 is evaluated. A side effect is that the variable name still exists after the loop has concluded and it has the value of the last element of vector that the loop was evaluated for.

3.2.6 switch

Technically speaking, switch is just another function, but its semantics are close to those of control structures of other programming languages.

The syntax is

```
switch (statement, list)
```

where the elements of *list* may be named. First, *statement* is evaluated and the result, *value*, obtained. If *value* is a number between 1 and the length of *list* then the corresponding element *list* is evaluated and the result returned. If *value* is too large or too small NULL is returned.

```
> x <- 3
> switch(x, 2+2, mean(1:10), rnorm(5))
[1] 2.2903605 2.3271663 -0.7060073 1.3622045 -0.2892720
> switch(2, 2+2, mean(1:10), rnorm(5))
[1] 5.5
> switch(6, 2+2, mean(1:10), rnorm(5))
NULL
```

If value is a character vector then the element of '...' with a name that exactly matches value is evaluated. If there is no match NULL is returned.

```
> y <- "fruit"
> switch(y, fruit = "banana", vegetable = "broccoli", meat = "beef")
[1] "banana"
```

A common use of switch is to branch according to the character value of one of the arguments to a function.

[1] 0.6086504

switch returns either the value of the statement that was evaluated or NULL if no statement was evaluated.

To choose from a list of alternatives that already exists switch may not be the best way to select one for evaluation. It is often better to use eval and the subset operator, [[, directly via eval(x[[condition]]).

3.3 Elementary arithmetic operations

In this section, we discuss the finer points of the rules that apply to basic operation like addition or multiplication of two vectors or matrices.

3.3.1 Recycling rules

If one tries to add two structures with a different number of elements, then the shortest is recycled to length of longest. That is, if for instance you add c(1, 2, 3) to a six-element vector then you will really add c(1, 2, 3, 1, 2, 3). If the length of the longer vector is not a multiple of the shorter one, a warning is given.

One exception is that when adding vectors to matrices, a warning is not given if the lengths are incompatible.

3.3.2 Propagation of names

propagation of names (first one wins, I think - also if it has no names?? —- first one *with names* wins, recycling causes shortest to lose names)

3.3.3 Dimensional attributes

(matrix+matrix, dimensions must match. vector+matrix: first recycle, then check if dims fit, error if not)

3.3.4 NA handling

Missing values in the statistical sense, that is, variables whose value is not known, have the value NA. This should not be confused with the missing property for a function argument that has not been supplied (see Section 4.1.2 [Arguments], page 21).

As the elements of a vector or matrix must be of the same type there are multiple types of NA values. There is one cases where this is particularly important to the user. The default type of NA is logical, unless coerced to some other type, so the appearance of a missing value may trigger logical rather than numeric indexing (see Section 3.4 [Indexing], page 16 for details).

Numeric and logical calculations with NA generally return NA. In cases where the result of the operation would be the same for all possible values the NA could take, the operation may return this value. In particular, 'FALSE & NA' is FALSE, 'TRUE | NA' is TRUE. NA is not equal to any other value or to itself; testing for NA is done using is.na.

Numeric calculations whose result is undefined, such as '0/0' produce (on most, if not all, platforms) the value NaN. This exists only in the double type. The function is.nan

is provided to check specifically for NaN, is.na also returns TRUE for NaN. Coercing NaN to logical or integer type gives an NA of the appropriate type.

The NA of character type is currently the string "NA", so this string cannot be used as a character value (eg as an abbreviation for "North America"). This may change in the future. Programmers who need to specify an explicit string NA should use 'as.character(NA)' rather than "NA".

3.4 Indexing

R contains several constructs which allow access to individual elements or subsets through indexing operations. In the case of the basic vector types one can access the i-th element using x[i], but there is also indexing of lists, matrices, and multi-dimensional arrays. There are several forms of indexing in addition to indexing with a single integer.

R has three basic indexing operators, with syntax displayed by the following examples

```
x[i]
x[i, j]
x[[i]]
x[[i, j]]
x$a
x$"a"
```

For vectors and matrices the [[forms are rarely used, although it has some slight semantic differences from the [form, in that it drops any names or dimnames attribute. When indexing multi-dimensional structures with a single index, x[[i]] or x[i] will return the ith sequential element of x.

For lists, one generally uses [[to select any single element, whereas [returns a list of the selected elements.

The [[form allows only a single element to be selected using integer or character indices, whereas [allows indexing by vectors.

The form using \$ applies to list object. It allows only a literal character string or a symbol as the index. That is, the index is not computable. For cases where you need to evaluate an expression to find the index, use x[[expr]].

3.4.1 Indexing by vectors

R allows some powerful constructions using vectors as indices. We shall discuss indexing of simple vectors first. For simplicity, assume that the expression is x[i]. Then the following possibilities exist according to the type of i.

• Integer. All elements of i must have the same sign. If they are positive, the elements of x with those index numbers are selected. If i contains negative elements, all elements except those indicated are selected.

If i is positive and exceeds length(x) then the corresponding selection is NA. A negative out of bounds value for i causes an error.

A special case is the zero index, which has null effects: x[0] is an empty vector and otherwise including zeros among positive or negative indices has the same effect as if they were omitted.

- Other numeric. Non-integer values are converted to integer before use.
- Logical. The indexing i should generally have the same length as x. If it is shorter, then its elements will be recycled as discussed in Section 3.3 [Elementary arithmetic operations], page 15. If it is longer, then x is conceptually extended with NAs. The selected values of x are those for which i is TRUE.
- ullet Character. The strings in i are matched against the names attribute of x and the resulting integers are used.
- Factor. The result is identical to x[as.integer(i)]. The factor levels are never used. If so desired, use x[as.character(i)] or a similar construction.
- Empty. The expression x[] returns x, but drops "irrelevant" attributes from the result. Only names and in multi-dimensional arrays dim and dimnames attributes are retained.

Indexing with a missing (i.e. NA) value give an NA result. This rule applies also to the case of logical indexing, i.e. the elements of x that have an NA selector in i get included in the result, but their value will be NA.

Notice however, that there are different modes of NA—the literal constant is of mode "logical", but it is frequently automatically coerced to other types. One effect of this is that x[NA] has the length of x, but x[c(1, NA)] has length 2. That is because the rules for logical indices apply in the former case, but those for integer indices in the latter.

Indexing with [will also carry out the relevant subsetting of any names attributes.

3.4.2 Indexing matrices and arrays

Subsetting multi-dimensional structures generally follows the same rules as single-dimensional indexing for each index variable, with the relevant component of dimnames taking the place of names. A couple of special rules apply, though:

Normally, a structure is accessed using the number of indices corresponding to its dimension. It is however also possible to use a single index in which case the dim and dimnames attributes are disregarded and the result is effectively that of c(m)[i]. Notice that m[1] is usually very different from m[1,] or m[, 1].

It is possible to use a matrix of integers as an index. In this case, the number of columns of the matrix should match the number of dimensions of the structure, and the result will be a vector with length as the number of columns of the matrix. The following example shows how to extract the elements m[1, 1] and m[2, 2] in one operation.

```
> m <- matrix(1:4, 2)
> m
     [,1] [,2]
[1,]
              3
        1
[2,]
> i <- matrix(c(1, 1, 2, 2), 2, byrow = TRUE)
> i
     [,1] [,2]
[1,]
        1
              1
[2,]
        2
              2
> m[i]
[1] 1 4
```

Both in the case of using a single index and in matrix indexing, a names attribute is used if present, as had the structure been one-dimensional.

If an indexing operation causes the result to have one of its extents of length one, as in selecting a single slice of a three-dimensional matrix with (say) m[2, ,], the corresponding dimension is generally dropped from the result. If a single-dimensional structure results, a vector is obtained. This is occasionally undesirable and can be turned off by adding the 'drop = FALSE' to the indexing operation. Notice that this is an additional argument to the [function and doesn't add to the index count. Hence the correct way of selecting the first row of a matrix as a 1 by n matrix is m[1, , drop = FALSE]. Forgetting to disable the dropping feature is a common cause of failure in general subroutines where an index occasionally, but not usually has length one. This rule still applies to one-dimensional array, where any subsetting will give a vector result unless 'drop = FALSE' is used.

Notice that vectors are distinct from one-dimensional arrays in that the latter have dim and dimnames attributes (both of length one). One-dimensional arrays are not easily obtained from subsetting operations but they can be constructed explicitly. This is sometimes useful because the elements of the dimnames list may themselves be named, which is not the case for the names attribute.

Some operations such as m[FALSE,] result in structures in which a dimension has zero extent. R generally tries to handle these structures sensibly.

3.4.3 Indexing other structures

The operator [is a generic function which allows class methods to be added, and the \$ and [[operators likewise. Thus, it is possible to have user-defined indexing operations for any structure. Such a function, say [.foo is called with a set of arguments of which the first is the structure being indexed and the rest are the indices. In the case of \$, the index argument is of mode "symbol" even when using the x\$"abc" form.

The most important example of a class method for [is that used for data frames. It is not be described in detail here, but in broad terms, it creates matrix-like indexing for a structure that is basically a list of vectors of the same length.

3.4.4 Subset assignment

subassignment

what is really going on is that... something about *tmp* (internally, R tries to avoid duplication as far as possible).

3.5 Scope of variables

Almost every programming language has a set of scoping rules, allowing the same name to be used for different objects. This allows, e.g., a local variable in a function to have the same name a global object.

R uses a *lexical scoping* model, similar to languages like Pascal. However, R is a *functional programming language* and allows dynamic creation and manipulation of functions and language objects, and has additional features reflecting this fact.

3.5.1 Global environment

The global environment is the root of the user workspace. An assignment operation from command line will cause the relevant object to belong to the global environment.

3.5.2 Lexical environment

Every call to a function creates a *frame* which contains the local variables created in the function, and is evaluated in an environment, which in combination creates a new environment.

Notice the terminology: A frame is a set of variables, an environment is a nesting of frames (or equivalently: the innermost frame plus the enclosing environment).

Environments may be assigned to variables or be contained in other objects. However, notice that they are not themselves objects—in particular, they are not copied on assignment.

A closure (mode "function") object will contain the environment in which it is created as part of its definition (By default. The environment can be manipulated using environment<-). When the function is subsequently called, its evaluation environment becomes nested in its definition environment. Notice that this is not necessarily the environment of the caller!

Thus, when a variable is requested inside a function, it is first sought in the evaluation environment, then in the enclosure, the enclosure of the enclosure, etc.

3.5.3 The call stack

Every time a function is invoked a new evaluation frame is created. At any point in time during the computation the the currently active environments are accessible through the call stack. Each time a function is invoked a special construct called a context is created internally and is placed on a list of contexts. When a function has finished evaluating its context is removed from the call stack.

Making variables defined higher up the call stack available is called dynamic scope. The binding for a variable is then determined by the most recent (in time) definition of the variable. This contradicts the default scoping rules in R, which use the bindings in the environment in which the function was defined (lexical scope). Some functions, particularly those that use and manipulate model formulas, need to simulate dynamic scope by directly accessing the call stack.

Access to the call stack is provided through a family of functions which have names that start with 'sys.'. They are listed briefly below.

sys.call Get the call for the specified context

sys.frame

Get the evaluation frame for the specified context.

sys.nframe

Get the environment frame for all active contexts.

sys.function

Get the function being invoked in the specified context.

sys.parent

Get the parent of the current function invocation.

sys.calls

Get the calls for all the active contexts.

sys.frames

Get the evaluation frames for all the active contexts.

sys.parents

Get the numeric labels for all active contexts.

sys.on.exit

Set a function to be executed when the specified context is exited.

sys.status

Calls sys.frames, sys.parents and sys.calls.

parent.frame

Get the evaluation frame for the specified parent context.

3.5.4 Search path

In addition to the evaluation environment structure, R has a search path of environments which are searched for variables not found elsewhere. This is used for two things: packages of functions and attached user data.

The first element of the search path is the global environment and the last is the base package. An Autoloads environment is used for holding proxy objects that may be loaded on demand. Other environments are inserted in the path using attach or library.

4 Functions

4.1 Writing functions

While R can be very useful as a data analysis tool most users very quickly find themselves wanting to write their own functions. This is one of the real advantages of R. Users can program it and they can, if they want to, change the system level functions to functions that they find more appropriate.

R also provides facilities that make it easy to document any functions that you have created. See section "Writing R documentation" in *Writing R Extensions*.

4.1.1 Syntax and examples

The syntax for writing a function is function (arglist) body

The first component of the function declaration is the keyword function which indicates to R that you want to create a function.

An argument list is a comma separated list of formal arguments. A formal argument can be a symbol, a statement of the form 'symbol = expression', or the special formal argument '...'.

The body can be any valid R expression. Generally, the body is a group of expressions contained in curly braces (' $\{$ ' and ' $\}$ ').

Generally functions are assigned to symbols but they don't need to be. The value returned by the call to function is a function. If this is not given a name it is referred to as an anonymous function. Anonymous functions are most frequently used as arguments other functions such as the apply family or outer.

Here is a simple function: echo <- function(x) print(x). So echo is a function that takes a single argument and when echo is invoked it prints its argument.

4.1.2 Arguments

The formal arguments to the function define the variables whose values will be supplied at the time the function is invoked. The names of these arguments can be used within the function body where they obtain the value supplied at the time of function invocation.

Default values for arguments can be specified using the special form 'name = expression'. In this case, if the user does not specify a value for the argument when the function is invoked the expression will be associated with the corresponding symbol. When a value is needed the expression is evaluated in the evaluation frame of the function.

Default behaviours can also be specified by using the function missing. When missing is called with the name of a formal argument it returns TRUE if the formal argument was not matched with any actual argument and has not been subsequently modified in the body of the function. A an argument that is missing will thus have its default value, if any. The missing function does not force evaluation of the argument.

The special type of argument '...' can contain any number of supplied arguments. It is used for a variety of purposes. It allows you to write a function that takes an arbitrary

number of arguments. It can be used to absorb some arguments into an intermediate function which can then be extracted by functions called subsequently.

4.2 Function objects

In R a function can be thought of as consisting of three parts. These are the *body*, the *formal arguments*, and the *environment*.

The *body* is the expression that is to be evaluated when the function is invoked. The *formal arguments* provide the mapping between the values that are supplied by the user and the symbols or names that appear in the body of the function. Finally, the *environment* is the environment that was active at the time that the function was created. This environment is associated with the function for the life of the function (unless it purposely removed).

Functions are first class objects in R. They can be used anywhere that an R object is required. In particular they can be passed as arguments to functions and returned as values from functions.

4.3 Evaluation

4.3.1 Evaluation environment

When a function is called or invoked a new evaluation frame is created. In this frame the formal arguments are matched with the supplied arguments according to the rules given in Section 4.3.2 [Argument matching], page 22. The statements in the body of the function are evaluated sequentially in this environment frame.

The parent or enclosing frame of the evaluation frame is the environment frame associated with the function being invoked. This may be different than S. While most functions have .GlobalEnv as their parent this does not have to be true.

4.3.2 Argument matching

The first thing that occurs in a function evaluation is the matching of formal to the actual or supplied arguments. This is done by a three-pass process:

- 1. **Exact matching on tags**. For each named supplied argument the list of formal arguments is searched for an item whose name matches exactly. It is an error to have the same formal argument match several actuals or vice versa.
- 2. Partial matching on tags. Each named supplied argument is compared to the remaining formal arguments using partial matching. If the name of the supplied argument matches exactly with the first part of a formal argument then the two arguments are considered to be matched. It is an error to have multiple partial matches. Notice that if f <-function(fumble, fooey) fbody, then f(f = 1, fo = 2) is illegal, even though the 2nd actual argument only matches fooey. f(f = 1, fooey = 2) is legal though since the second argument matches exactly and is removed from consideration for partial matching. If the formal arguments contain '...' then partial matching is only applied to arguments that precede it.

3. **Positional matching**. Any unmatched formal arguments are bound to *unnamed* supplied arguments, in order. If there is a '...' argument, it will take up the remaining arguments, tagged or not.

If any arguments remain unmatched an error is declared.

Argument matching is augmented by the functions match.arg, match.call and match.fun. Access to the partial matching algorithm used by R is via pmatch.

4.3.3 Argument evaluation

One of the most important things to know about the evaluation of arguments to a function is that supplied arguments and default arguments are treated differently. The supplied arguments to a function are evaluated in the evaluation frame of the calling function. The default arguments to a function are evaluated in the evaluation frame of the function.

The semantics of invoking a function in R argument are *call-by-value*. In general, supplied arguments behave as if they are local variables initialized with the value supplied and the name of the corresponding formal argument. Changing the value of a supplied argument within a function will not affect the value of the variable in the calling frame.

R has a form of lazy evaluation of function arguments. Arguments are not evaluated until needed. It is important to realize that in some cases the argument will never be evaluated. Thus, it is bad style to use arguments to functions to cause side-effects. While in C it is common to use the form, foo(x = y) to invoke foo with the value of y and simultaneously to assign the value of y to x this same style should not be used in R. There is no guarantee that the argument will ever be evaluated and hence the assignment may not take place.

It is also worth noting that the effect of $foo(x \le y)$ if the argument is evaluated is to change the value of x in the calling environment and not in the evaluation environment of foo.

It is possible to access the actual expressions used as arguments inside the function. The mechanism is implemented via promises. A promise is a data structure that is not available to the user in R. However, understanding how promises work should help to write better code. When a function is being evaluated the actual expression used as an argument is stored in the promise together with a pointer to the environment the function was called from. When (if) the argument is evaluated the stored expression is evaluated in the environment that the function was called from. Since only a pointer to the environment is used any changes made to that environment will be in effect during this evaluation. The resulting value is then also stored in a separate spot in the promise. Subsequent evaluations retrieve this stored value (a second evaluation is not carried out). Access to the unevaluated expression is also available (in internal code). Because R is a very flexible program it is possible to encounter promises in the interpreted language, however, users are advised not to rely on them in their own programs.

When a function is called, each formal argument is assigned a promise in the local environment of the call with the expression slot containing the actual argument and the environment slot containing the environment of the parent. If no actual argument for a formal argument is given in the call and there is a default expression, it is similarly assigned to the expression slot of the formal argument, but with the environment set to the local environment.

The process of filling the value slot of a promise by evaluating the contents of the expression slot in the promises environment is called *forcing* the promise. A promise will only be forced once, the value slot content being used directly later on.

A promise is forced when its value is needed. This usually happens inside internal functions, but a promise can also be forced by direct evaluation of the promise itself. This is occasionally useful when a default expression depends on the value of another formal argument. This is seen in the following example where the lone label ensures that the label is based on the argument expression.

```
function(x, label = deparse(x)) {
    label
    x <- x + 1
    print(label)
}</pre>
```

The expression slot of a promise can itself involve other promises. This happens whenever an unevaluated argument is passed as an argument to another function. When forcing a promise, all other promises in its expression will also be forced recursively.

4.3.4 Scope

Scope or the scoping rules are simply the set of rules used by the evaluator to find a value for a symbol. Every computer language has a set of such rules. In R the rules are fairly simple but there do exist mechanisms for subverting the usual, or default rules.

R adheres to a set of rules that are called *lexical scope*. This means the variable bindings in effect at the time the expression was created are used to provide values for any unbound symbols in the expression.

Most of the interesting properties of scope are involved with evaluating functions and we concentrate on this issue. A symbol can be either bound or unbound. All of the formal arguments to a function provide bound symbols in the body of the function. Any other symbols in the body of the function are either local variables or unbound variables. A local variable is one that is defined within the function. Because R has no formal definition of variables, they are simply used as needed, it can be difficult to determine whether a variable is local or not. Local variables must first be defined, this is typically done by having them on the left-hand side of an assignment.

During the evaluation process if an unbound symbol is detected then R attempts to find a value for it. The scoping rules determine how this process proceeds. In R the environment of the function is searched first, then its parent and so until top-level is reached.

Top-level is a search list of environments that are searched sequentially for the symbol. The first value found is then used.

When this set of rules is combined with the fact that functions can be returned as values from other functions then some rather nice, but at first glance peculiar, properties obtain.

A simple example,

```
f <- function(x) {
    y <- 10
    g <- function(x) x + y
    return(g)</pre>
```

A rather interesting question is what happens when h is evaluated. To describe this we need a bit more notation. Within a function body variables can be bound, local or unbound. The bound variables are those that match the formal arguments to the function. The local variables are those that were created or defined within the function body. The unbound variables are those that are neither local or bound. When a function body is evaluated there is no problem determining values for local variables or for bound variables. Scoping rules determine how the language will find values for the unbound variables.

When h(3) is evaluated we see that its body is that of g. Within that body x and y are unbound. In a language with lexical scope x will be associated with the value 3 and y with the value 10 so h() should return the value 13. In R this is indeed what happens.

In S, because of the different scoping rules one will get an error indicating that y is not found, unless there is a variable y in your workspace in which case its value will be used.

The scoping rules in S are to look in the current frame and then in the global environment or workspace. These rules are very similar to the scoping rules used in the C language.

4.4 Closures

A *closure* is a function together with an environment that provides bindings for any free variables in the closure. Since many R functions are bound to environments they are often referred to as closures.

5 Object-oriented programming

Object-oriented programming is a style of programming that has become popular in recent years. Much of the popularity comes from the fact that it makes it easier to write and maintain complicated systems. It does this through several different mechanisms.

Central to any object-oriented language are the concepts of class and of methods. A class is a definition of an object. Typically a class contains several slots that are used to hold class-specific information. An object in the language must be an instance of some class. Programming is based on objects or instances of classes.

Computations are carried out via *methods*. Methods are basically functions that are specialized to carry out specific calculations on objects, usually of a specific class. This is what makes the language object oriented. In R, *generic functions* are used to determine the appropriate method. The generic function is responsible for determining the class of its argument(s) and uses that information to select the appropriate method.

Another feature of most object-oriented languages is the concept of inheritance. In most programming problems there are usually many objects that are related to one another. The programming is considerably simplified if some components can be reused.

If a class inherits from another class then generally it gets all the slots in the parent class and can extend it by adding new slots. On method dispatching (via the generic functions) if a method for the class does not exist then a method for the parent is sought.

In this chapter we discuss how this general strategy has been implemented in R and discuss some of the limitations within the current design. One of the advantages that most object systems impart is greater consistency. This is achieved via the rules that are checked by the compiler or interpretor. Unfortunately because of the way that the object system is incorporated into R this advantage does not obtain. Users are cautioned to use the object system in a straightforward manner. While it is possible to perform some rather interesting feats these tend to lead to obfuscated code and may depend on implementation details that will not be carried forward.

The greatest use of object oriented programming in R is through print methods, summary methods and plot methods. These methods allow us to have one generic function call, plot say, that dispatches on the type of its argument and calls a plotting function that is specific to the data supplied.

In order to make the concepts clear we will consider the implementation of a small system designed to teach students about probability. In this system the objects are probability functions and the methods we will consider are methods for finding moments and for plotting. Probabilities can always be represented in terms of the cumulative distribution function but can often be represented in other ways. For example as a density, when it exists or as a moment generating function when it exists.

5.1 Definition

Rather than having a full-fledged object-oriented system R has a class system and a mechanism for dispatching based on the class of an object. The dispatch mechanism for interpreted code relies on four special objects that are stored in the evaluation frame. These

special objects are .Generic, .Class, .Method and .Group. There is a separate dispatch mechanism used for internal functions and types that will be discussed elsewhere.

The class system is facilitated through the class attribute. This attribute is a list of class names. So to create an object of class "foo" one simply attaches a class attribute with the string '"foo" in it. Thus, virtually anything can be turned in to an object of class "foo"

The object system makes use of *generic functions* via two dispatching functions, UseMethod and NextMethod. The typical use of the object system is to begin by calling a generic function. This is typically a function is very simple and consists of a single line of code. The system function mean is just such a function,

```
> mean
function (x, ...)
UseMethod("mean")
```

When mean is called it can have any number of arguments but its first argument is special and the class of that first argument is used to determine which method should be called. The variable .Class is set to the class attribute of x, .Generic is set to the string "mean" and a search is made for the correct method to invoke. The class attributes of any other arguments to mean are ignored.

Suppose that x had a class attribute that contained "foo" and "bar", in that order. Then R would first search for a function called mean.foo and if it did not find one it would then search for a function mean.bar and if that search was also unsuccessful then a final search for foo.default would be made. If the last search is unsuccessful R reports an error. It is a good idea to always write a default method. Note that the functions mean.foo etc. are referred to, in this context, as methods.

NextMethod provides another mechanism for dispatching. A function may have a call to NextMethod anywhere in it. The determination of which method should then be invoked is based primarily on the current values of .Class and .Generic. This is somewhat problematic since the method is really an ordinary function and users may call it directly. If they do so then there will be no values for .Generic or .Class.

If a method is invoked directly and it contains a call to NextMethod then the first argument to NextMethod is used to determine the generic function. An error is signalled if this argument has not been supplied; it is therefore a good idea to always supply this argument.

In the case that a method is invoked directly the class attribute of the first argument to the method is used as the value of .Class.

Methods themselves employ NextMethod to provide a form of inheritance. Commonly a specific method performs a few operations to set up the data and then it calls the next appropriate method through a call to NextMethod.

Consider the following simple example. A point in two-dimensional Euclidean space can be specified by its Cartesian (x-y) or polar (r-theta) coordinates. Hence, to store information about the location of the point, we could define two classes, "xypoint" and "rthetapoint". All the 'xypoint' data structures are lists with an x-component and a y-component. All 'rthetapoint' objects are lists with an r-component and a theta-component.

Now, suppose we want to get the x-position from either type of object. This can easily be achieved through generic functions. We define the generic function xpos as follows.

```
xpos <- function(x, ...)
     UseMethod("xpos")

Now we can define methods:
     xpos.xypoint <- function(x) x$x
     xpos.rthetapoint <- function(x) x$r * cos(x$theta)</pre>
```

The user simply calls the function **xpos** with either representation as the argument. The internal dispatching method finds the class of the object and calls the appropriate methods.

It is pretty easy to add other representations. One need not write a new generic function only the methods. This makes it easy to add to existing systems since the user is only responsible for dealing with the new representation and not with any of the existing representations.

The bulk of the uses of this methodology are to provided specialized printing for objects of different types; there are about 40 methods for print.

5.2 Inheritance

The class attribute of an object can have several elements. When a generic function is called the first inheritance is mainly handled through NextMethod. NextMethod determines the method currently being evaluated, finds the next class from th

FIXME: something is missing here

5.3 Method dispatching

Generic functions should consist of a single statement. They should always be of the form foo <- function(x, ...) UseMethod("foo", x). The semantics of UseMethod are an appropriate method is determined and then that method is invoked with the same arguments, in the same order as the call to the generic as if the call had been made directly to the method.

In order to determine the correct method the class attribute of the first argument to the generic is obtained and used to find the correct method. The name of the generic function is combined with the first element of the class attribute into the form, generic. class and a function with that name is sought. If the function is found then it is used. If no such function is found then the second element of the class attribute is used, and so on until all the elements of the class attribute have been exhausted. If no method has been found at that point then the method generic. default is used. If the first argument to the generic function has no class attribute then generic. default is used.

Any object can have a **class** attribute. This attribute can have any number of elements. Each of these is a string that defines a class. When a generic function is invoked the class of its first argument is examined.

5.4 UseMethod

UseMethod is a special function and it behaves differently from other function calls. The syntax of a call to it is UseMethod(generic, object), where generic is the name of the generic function, object is the object used to determine which method should be chosen. UseMethod

can only be called from inside a function. The S definition of UseMethod contains an additional argument of '...' that appears to have no effect on any subsequent computations. R produces a warning if there are more than two arguments to UseMethod and ignores these additional arguments.

UseMethod changes the evaluation model in two ways. First, when it is invoked it determines the next method (function) to be called. It then invokes that function using the current evaluation environment; this process will be described shortly. The second way in which UseMethod changes the evaluation environment is that it does not return control to the calling function. This means, that any statements after a call to UseMethod are guaranteed not to be executed.

When UseMethod is invoked the generic function is determined as either the specified value in the call to UseMethod or as the name of the current function if no value was specified. The object to dispatch on is either the supplied second argument or the first argument to the current function. The class of the argument is determined and the first element of it is combined with the name of the generic to determine the appropriate method. So, if the generic had name foo and the class of the object is "bar", then R will search for a method named foo.bar. If no such method exists then the inheritance mechanism described above is used to locate an appropriate method.

Once a method has been determined R invokes it in a special way. Rather than creating a new evaluation environment R uses the environment of the current function call (the call to the generic). Any assignments or evaluations that were made before the call to UseMethod will be in effect. The arguments that were used in the call to the generic are rematched to the formal arguments of the selected method.

When the method is invoked it is called with arguments that are the same in number and have the same names as in the call to the generic. They are matched to the arguments of the method according to the standard R rules for argument matching. However the object, i.e. the first argument has been evaluated.

The call to UseMethod has the effect of placing some special objects in the evaluation frame. They are .Class, .Generic and .Method. These special objects are used to by R to handle the method dispatch and inheritance. .Class is the class of the object, .Generic is the name of the generic function and .Method is the name of the method currently being invoked. If the method was invoked through one of the internal interfaces then there may also be an object called .Group. This will be described in Section Section 5.6 [Group methods], page 31. After the initial call to UseMethod these special variables, not the object itself, control the selection of subsequent methods.

The body of the method is then evaluated in the standard fashion. In particular variable look-up in the body follows the rules for the method. So if the method has an associated environment then that is used. In effect we have replaced the call to the generic by a call to the method. Any local assignments in the frame of the generic will be carried forward into the call to the method. Use of this *feature* is discouraged. It is important to realize that control will never return to the generic and hence any expressions after a call to UseMethod will never be executed.

Any arguments to the generic that were evaluated prior to the call to <code>UseMethod</code> remain evaluated.

The arguments in the call to the generic are rematched with the arguments for the method using the standard argument matching mechanism. The first argument, i.e. the object, will have been evaluated.

If the first argument to UseMethod is not supplied it is assumed to be the name of the current function. If two arguments are supplied to UseMethod then the first is the name of the method and the second is assumed to be the object that will be dispatched on. It is evaluated so that the required method can be determined. In this case the first argument in the call to the generic is not evaluated and is discarded. There is no way to change the other arguments in the call to the method these remain as they were in the call to the generic. This is in contrast to NextMethod where the arguments in the call to the next method can be altered.

5.5 NextMethod

NextMethod is used to provide a simple inheritance mechanism.

Methods invoked as a result of a call to NextMethod behave as if they had been invoked from the previous method. The arguments to the inherited method are in the same order and have the same names as the call to the current method. This means that they are the same as for the call to the generic. However, the expressions for the arguments are the names of the corresponding formal arguments of the current method. Thus the arguments will have values that correspond to their value at the time NextMethod was invoked.

Unevaluated arguments remain unevaluated. Missing arguments remain missing.

The syntax for a call to NextMethod is NextMethod(generic, object, ...). If the generic is not supplied the value of .Generic is used. If the object is not supplied the first argument in the call to the current method is used. Values in the '...' argument are used to modify the arguments of the next method.

It is important to realize that the choice of the next method depends on the current values of .Generic and .Class and not on the object. So changing the object in a call to NextMethod affects the arguments received by the next method but does not affect the choice of the next method.

Methods can be called directly. If they are then there will be no .Generic, .Class or .Method. In this case the generic argument of NextMethod must be specified. The value of .Class is taken to be the class attribute of the object which is the first argument to the current function. The value of .Method is the name of the current function. These choices for default values ensure that the behaviour of a method doesn't change depending on whether it is called directly or via a call to a generic.

An issue for discussion is the behaviour of the '...' argument to NextMethod. The White Book describes the behaviour as follows:

- named arguments replace the corresponding arguments in the call to the current method. Unnamed arguments go at the start of the argument list.

What I would like to do is:

-first do the argument matching for NextMethod; -if the object or generic are changed fine -first if a named list element matches an argument (named or not) the list value replaces the argument value. - the first unnamed list element

Values for lookup: Class: comes first from .Class, second from the first argument to the method and last from the object specified in the call to NextMethod

Generic: comes first from .Generic, if nothing then from the first argument to the method and if it's still missing from the call to NextMethod

Method: this should just be the current function name.

5.6 Group methods

For several types of built-in functions R provides a dispatching mechanism for operators. This means that operators such as == or < can have their behaviour modified for members of special classes. The functions and operators have been grouped into three categories and group methods can be written for each of these categories. There is currently no mechanism to add groups. It is possible to write methods specific to any function within a group.

The following table lists the functions for the different Groups.

'Math' abs, acos, acosh, asin, asinh, atan, atanh, ceiling, cos, cosh, cumsum, exp, floor, gamma, lgamma, log, log10, round, signif, sin, sinh, tan, tanh, trunc

'Summary' all, any, max, min, prod, range, sum

For operators in the Ops group a special method is invoked if the two operands taken together suggest a single method. Specifically, if both operands correspond to the same method or if one operand corresponds to a method that takes precedence over that of the other operand. If they do not suggest a single method then the default method is used. Either a group method or a class method dominates if the other operand has no corresponding method. A class method dominates a group method.

When the group is Ops the special variable .Method is a string vector with two elements. The elements of .Method are set to the name of the method if the corresponding argument is a member of the class that was used to determine the method. Otherwise the corresponding element of .Method is set to the zero length string, "".

5.7 Writing methods

Users can easily write their own methods and generic functions. A generic function is simply a function with a call to UseMethod. A method is simply a function that has been invoked via method dispatch. This can be as a result of a call to either UseMethod or NextMethod.

It is worth remembering that methods can be called directly. That means that they can be entered without a call to UseMethod having been made and hence the special variables .Generic, .Class and .Method will not have been instantiated. In that case the default rules detailed above will be used to determine these.

The most common use of generic functions is to provide print and summary methods for statistical objects, generally the output of some model fitting process. To do this, each model attaches a class attribute to its output and then provides a special method that takes that output and provides a nice readable version of it. The user then needs only remember that print or summary will provide nice output for the results of any analysis.

6 Computing on the language

R belongs to a class of programming languages in which subroutines have the ability to modify or construct other subroutines and evaluate the result as an integral part of the language itself. This is similar to Lisp and Scheme and other languages of the "functional programming" variety, but in contrast to FORTRAN and the ALGOL family. The Lisp family takes this feature to the extreme by the "everything is a list" paradigm in which there is no distinction between programs and data.

R presents a friendlier interface to programming than Lisp does, at least to someone used to mathematical formulas and C-like control structures, but the engine is really very Lisp-like. R allows direct access to parsed expressions and functions and allows you to alter and subsequently execute them, or create entirely new functions from scratch.

There is a number of standard applications of this facility, such as calculation of analytical derivatives of expressions, or the generation of polynomial functions from a vector of coefficients. However, there are also uses that are much more fundamental to the workings of the interpreted part of R. Some of these are essential to the reuse of functions as components in other functions, as the (admittedly not very pretty) calls to model.frame that are constructed in several modeling and plotting routines. Other uses simply allow elegant interfaces to useful functionality. As an example, consider the curve function, which allows you to draw the graph of a function given as an expression like sin(x) or the facilities for plotting mathematical expressions.

In this chapter, we give an introduction to the set of facilities that are available for computing on the language.

6.1 Direct manipulation of language objects

There are three kinds of language objects that are available for modification, calls, expressions, and functions. At this point, we shall concentrate on the call objects. These are sometimes referred to as "unevaluated expressions", although this terminology is somewhat confusing. The most direct method of obtaining a call object is to use quote with an expression argument, e.g.,

```
> e1 <- quote(2 + 2)
> e2 <- quote(plot(x, y))</pre>
```

The arguments are not evaluated, the result is simply the parsed argument. The objects e1 and e2 may be evaluated later using eval, or simply manipulated as data. It is perhaps most immediately obvious why the e2 object has mode "call", since it involves a call to the plot function with some arguments. However, e1 actually has exactly the same structure as a call to the binary operator + with two arguments, a fact that gets clearly displayed by the following

```
> quote("+"(2, 2))
2 + 2
```

The components of a call object are accessed using a list-like syntax, and may in fact be converted to and from lists using as.list and as.call

```
> e2[[1]]
plot
```

```
> e2[[2]]
x
> e2[[3]]
y
```

When keyword argument matching is used, the keywords can be used as list tags:

```
> e3 <- quote(plot(x = age, y = weight))
> e3$x
age
> e3$y
weight
```

All the components of the call object have mode "name" in the preceding examples. This is true for identifiers in calls, but the components of a call can also be constants—which can be of any type, although the first component had better be a function if the call is to be evaluated successfully—or other call objects, corresponding to subexpressions. Objects of mode name can be constructed from character strings using as.name, so one might modify the e2 object as follows

```
> e2[[1]] <- as.name("+")
> e2
x + y
```

To illustrate the fact that subexpressions are simply components that are themselves calls, consider

```
> e1[[2]] <- e2
> e1
x + y + 2
```

One thing to note is that R's departer does not parenthesize expressions. If you for instance do

```
> e1 <- quote(4 - 2)
> e1[[3]] <- quote(2 - 2) # replacing the '2'
> e1
4 - 2 - 2
```

then e1 is really 4 - (2 - 2) and not (4 - 2) - 2 as the left-associative rule would suggest. This reveals itself when you evaluate the call using

```
> eval(e1)
[1] 4
```

All grouping parentheses in input are preserved in parsed expressions. They are represented as a function call with one argument, so that 4 - (2 - 2) becomes "-"(4, "("("-"(2, 2))) in prefix notation. In evaluations, the '('operator just returns its argument.

This is a bit unfortunate, but it is not easy to write a parser/deparser combination that both preserves user input, stores it in minimal form and ensures that parsing a deparsed expression gives the same expression back.

As it happens, R's parser is not perfectly invertible, nor is its deparser, as the following examples show

```
> deparse(quote(c(1, 2)))
[1] "c(1, 2)"
> deparse(1:2)
```

```
[1] "c(1, 2)"
> quote("-"(2, 2))
2 - 2
> quote(2 - 2)
2 - 2
```

The parser/deparser system does, however, make a fairly good job on basic expressions.

...internal storage of flow control constructs...note Splus incompatibility...

6.2 Substitutions

It is in fact not often that one wants to modify the innards of an expression like in the previous section. More frequently, one wants to simply get at an expression in order to deparse it and use it for labeling plots, for instance. An example of this is seen at the beginning of plot.default:

```
xlabel <- if (!missing(x))
    deparse(substitute(x))</pre>
```

This causes the variable or expression given as the x argument to plot to be used for labeling the x-axis later on.

The function used to achieve this is substitute which takes the expression x and substitutes the expression that was passed through the formal argument x. Notice that for this to happen, x must carry information about the expression that creates its value. This is related to the lazy evaluation scheme of R (see Section 2.1.8 [Promise objects], page 5). A formal argument is really a *promise*, an object with two slots, one for the expression that defines it, and one for the value of that expression. substitute will recognize a promise variable and substitute the value of its expression slot. If substitute is invoked inside a function, the local variables of the function are also subject to substitution.

The argument to substitute does not have to be a simple identifier, it can be an expression involving several variables and substitution will occur for each of these. Also, substitute has an additional argument which can be an environment or a list in which the variables are looked up. For example:

```
> substitute(a + b, list(a = 1, b = quote(x)))
1 + x
```

Notice that quoting was necessary to substitute the x. This kind of construction comes in handy in connection with the facilities for putting math expression in graphs, as the flowing case shows

```
> plot(0)
> for (i in 1:4)
+ text(1, 0.2 * i,
+ substitute(x[ix] == y, list(ix = i, y = pnorm(i))))
```

It is important to realize that the substitutions are purely lexical; there is no checking that the resulting call objects make sense if they are evaluated. substitute(x <- x + 1, list(x = 2)) will happily return 2 <- 2 + 1. However, some parts of R make up their own rules for what makes sense and what does not and might actually have a use for such ill-formed expressions. For example, using the "math in graphs" feature often involves

constructions that are syntactically correct, but which would be meaningless to evaluate, like $\{\}>=40*"$ years".

Substitute will not evaluate its first argument. This leads to the puzzle of how to do substitutions on an object that is contained in a variable. The solution is to use substitute once more, like this

```
> expr <- quote(x + y)
> substitute(substitute(e, list(x = 3)), list(e = expr))
substitute(x + y, list(x = 3))
> eval(substitute(substitute(e, list(x = 3)), list(e = expr)))
3 + y
```

The exact rules for substitutions are as follows: Each symbol in the parse tree for the first is matched against the second argument, which can be a tagged list or an environment frame. If it is a simple local object, its value is inserted, except if matching against the global environment. If it is a promise (usually a function argument), the promise expression is substituted. If the symbol is not matched, it is left untouched. The special exception for substituting at the top level is admittedly peculiar. It has been inherited from S and the rationale is most likely that there is no control over which variables might be bound at that level so that it would be better to just make substitute act as quote.

The rule of promise substitution is slightly different from that of S if the local variable is modified before substitute is used. R will then use the new value of the variable, where as S will unconditionally use the argument expression—unless it was a constant, which has the curious consequence that f((1)) may be very different from f(1) in S. The R rule is considerably cleaner, although it does have consequences in connection with lazy evaluation that comes as a surprise to some. Consider

```
logplot <- function(y, ylab = deparse(substitute(y))) {
    y <- log(y)
    plot(y, ylab = ylab)
}</pre>
```

This looks straightforward, but one will discover that the y label becomes an ugly c(...) expression. It happens because the rules of lazy evaluation causes the evaluation of the ylab expression to happen *after* y has been modified. The solution is to force ylab to be evaluated first, i.e.,

```
logplot <- function(y, ylab = deparse(substitute(y))) {
    ylab
    y <- log(y)
    plot(y, ylab = ylab)
}</pre>
```

Notice that one should not use eval(ylab) in this situation. If ylab is a language or expression object, then that would cause the object to be evaluated as well, which would not at all be desirable if a math expression like quote(log[e](y)) was being passed.

6.3 More on evaluation

The eval function was introduced earlier in this chapter as a means of evaluating call objects. However, this is not the full story. It is also possible to specify the environment

in which the evaluation is to take place, by default this is the evaluation frame from which eval is called, but quite frequently it needs to be set to something else.

Very often, the relevant evaluation frame is that of the parent of the current frame (cf. ???). In particular, when the object to evaluate is the result of a substitute operation of the function arguments, it will contain variables that make sense to the caller only (notice that there is no reason to expect that the variables of the caller are in the lexical scope of the callee). Since evaluation in the parent frame occurs frequently, an eval.parent function exists as a shorthand for eval(expr, sys.frame(sys.parent())).

Another case that occurs frequently is evaluation in a list or a data frame. For instance, this happens in connection with the model.frame function when a data argument is given. Generally, the terms of the model formula need to be evaluated in data, but they may occasionally also contain references to items in the caller of model.frame. This is sometimes useful in connection with simulation studies. So for this purpose one needs not only to evaluate an expression in a list, but also to specify an enclosure into which the search continues if the variable is not in the list. Hence, the call has the form

```
eval(expr, data, sys.frame(sys.parent()))
```

Notice that evaluation in a given environment may actually change that environment, most obviously in cases involving the assignment operator, such as

```
eval(quote(total <- 0), environment(robert$balance)) # rob Rob
```

This is also true when evaluating in lists, but the original list does not change because one is really working on a copy.

6.4 Evaluation of expression objects

Objects of mode "expression" are defined in Section 2.1.4 [Expression objects], page 4. They are very similar to lists of call objects.

```
> ex <- expression(2 + 2, 3 + 4)
> ex[[1]]
2 + 2
> ex[[2]]
3 + 4
> eval(ex)
[1] 7
```

Notice that evaluating an expression object evaluates each call in turn, but the final value is that of the last call. In this respect it behaves almost identically to the compound language object quote({2 + 2; 3 + 4}). However, there is a subtle difference: Call objects are indistinguishable from subexpressions in a parse tree. This means that they are automatically evaluated in the same way a subexpression would be. Expression objects can be recognized during evaluation and in a sense retain their quotedness. The evaluator will not evaluate an expression object recursively, only when it is passed directly to eval function as above. The difference can be seen like this:

```
> eval(substitute(mode(x), list(x = quote(2 + 2))))
[1] "numeric"
> eval(substitute(mode(x), list(x = expression(2 + 2))))
[1] "expression"
```

The departer represents an expression object by the call that creates it. This is similar to the way it handles numerical vectors and several other objects that do not have a specific external representation. However, it does lead to the following bit of confusion:

```
> e <- quote(expression(2 + 2))
> e
expression(2 + 2)
> mode(e)
[1] "call"
> ee <- expression(2 + 2)
> ee
expression(2 + 2)
> mode(ee)
[1] "expression"
```

I.e., e and ee look identical when printed, but one is a call that generates an expression object and the other is the object itself.

6.5 Manipulation of function calls

It is possible for a function to find out how it has been called by looking at the result of sys.call as in the following example of a function that simply returns its own call:

```
> f <- function(x, y, ...) sys.call()
> f(y = 1, 2, z = 3, 4)
f(y = 1, 2, z = 3, 4)
```

However, this is not really useful except for debugging because it requires the function to keep track of argument matching in order to interpret the call. For instance, it must be able to see that the 2nd actual argument gets matched to the first formal one (\mathbf{x} in the above example).

More often one requires the call with all actual arguments bound to the corresponding formals. To this end, the function match.call is used. Here's a variant of the preceding example, a function that returns its own call with arguments matched

```
> f <- function(x, y, ...) match.call()
> f(y = 1, 2, z = 3, 4)
f(x = 2, y = 1, z = 3, 4)
```

Notice that the second argument now gets matched to \mathbf{x} and appears in the corresponding position in the result.

The primary use of this technique is to call another function with the same arguments, possibly deleting some and adding others. A typical application is seen at the start of the lm function:

```
mf <- cl <- match.call()
mf$singular.ok <- mf$model <- mf$method <- NULL
mf$x <- mf$y <- mf$qr <- mf$contrasts <- NULL
mf$drop.unused.levels <- TRUE
mf[[1]] <- as.name("model.frame")
mf <- eval(mf, sys.frame(sys.parent()))</pre>
```

Notice that the resulting call is evaluated in the parent frame, in which one can be certain that the involved expressions make sense. The call can be treated as a list object where

the first element is the name of the function and the remaining elements are the actual argument expressions, with the corresponding formal argument names as tags. Thus, the technique to eliminate undesired arguments is to assign NULL, as seen in lines 2 and 3, and to add an argument one uses tagged list assignment (here to pass drop.unused.levels = TRUE) as in line 4. To change the name of the function called, assign to the first element of the list and make sure that the value is a name, either using the as.name("model.frame") construction here or quote(model.frame).

The match.call function has an expand.dots argument which is a switch which if set to FALSE lets all '...' arguments be collected as a single argument with the tag '...'.

```
> f <- function(x, y, ...) match.call(expand.dots = FALSE)
> f(y = 1, 2, z = 3, 4)
f(x = 2, y = 1, ... = list(z = 3, 4))
The '...' argument is a list (a pairlist to be precise), not a call to list like it is in S:
> e1 <- f(y = 1, 2, z = 3, 4)$...
> e1
$z
[1] 3
[[2]]
[1] 4
```

One reason for using this form of match.call is simply to get rid of any '...' arguments in order not to be passing unspecified arguments on to functions that may not know them. Here's an example paraphrased from plot.formula:

```
m <- match.call(expand.dots = FALSE)
m$... <- NULL
m[[1]] <- "model.frame"</pre>
```

A more elaborate application is in update.default where a set of optional extra arguments can add to, replace, or cancel those of the original call:

```
extras <- match.call(expand.dots = FALSE)$...
if (length(extras) > 0) {
    existing <- !is.na(match(names(extras), names(call)))
    for (a in names(extras)[existing]) call[[a]] <- extras[[a]]
    if (any(!existing)) {
        call <- c(as.list(call), extras[!existing])
        call <- as.call(call)
    }
}</pre>
```

Notice that care is taken to modify existing arguments individually in case extras[[a]] == NULL. Concatenation does not work on call objects without the coercion as shown; this is arguably a bug.

Two further functions exist for the construction of function calls, namely call and do call

The function call allows creation of a call object from the function name and the list of arguments

```
> x <- 10.5
```

```
> call("round", x)
round(10.5)
```

As seen, the value of x rather than the symbol is inserted in the call, so it is distinctly different from round(x). The form is used rather rarely, but is occasionally useful where the name of a function is available as a character variable.

The function do.call is related, but evaluates the call immediate and takes the arguments from an object of mode "list" containing all the arguments. A natural use of this is when one wants to apply a function like cbind to all elements of a list or data frame.

```
is.na.data.frame <- function (x) {
   y <- do.call("cbind", lapply(x, "is.na"))
   rownames(y) <- row.names(x)
   y
}</pre>
```

Other uses include variations over constructions like do.call("f", list(...)). However, one should be aware that this involves evaluation of the arguments before the actual function call, which may defeat aspects of lazy evaluation and argument substitution in the function itself. A similar remark applies to the call function.

6.6 Manipulation of functions

It is often useful to be able to manipulate the components of a function or closure. R provides a set of interface functions for this purpose.

body Returns the expression that is the body of the function.

formals Returns a list of the formal arguments to the function. This is a pairlist.

environment

Returns the environment associated with the function.

body<- This sets the body of the function to the supplied expression.

formals<-

Sets the formal arguments of the function to the supplied list.

environment<-

Sets the environment of the function to the specified environment.

It is also possible to alter the bindings of different variables in the environment of the function, using code along the lines of $evalq(x \leftarrow 5, environment(f))$.

It is also possible to convert a function to a list using as.list. The result is the concatenation of the list of formal arguments with the function body. Conversely such a list can be converted to a function using as.function. This functionality is mainly included for S compatibility. Notice that environment information is lost when as.list is used, whereas as.function has an argument that allows the environment to be set.

7 System and foreign language interfaces

7.1 Operating system access

Access to the operating system shell is via the R function system. The details will differ by platform (see the on-line help), and about all that can safely be assumed is that the first argument will be a string command that will be passed for execution (not necessarily by a shell) and the second argument will be internal which if true will collect the output of the command into an R character vector.

The functions system.time and proc.time are available for timing (although the information available may be limited on non-Unix-like platforms).

Information from the operating system environment can be accessed and manipulated with

Sys.getenv OS environment variables

Sys.putenv

Sys.getlocale System locale

Sys.putlocale

Sys.localeconv
Sys.time Current time
Sys.timezone Time zone

A uniform set of file access functions is provided on all platforms:

file.access Ascertain File Accessibility

file.append Concatenate files

file.choose Prompt user for file name

file.copy Copy files

file.create Create or truncate a files

file.exists Test for existence

file.info Miscellaneous file information

file.remove remove files
file.show Display a text file

unlink Remove files or directories.

There are also functions for manipulating file names and paths in a platform-independent way.

basename File name without directory

dirname Directory name
file.path Construct path to file
path.expand Expand ~ in Unix path

7.2 Foreign language interfaces

See section "System and foreign language interfaces" in $Writing\ R$ Extensions for the details of adding functionality to R via compiled code.

Functions .C and .Fortran provide a standard interface to compiled code that has been linked into R, either at build time or via dyn.load. They are primarily intended for

compiled ${\bf C}$ and FORTRAN code respectively, but the .C function can be used with other languages which can generate C interfaces, for example C++.

Functions .Call and .External provide interfaces which allow compiled code (primarily compiled ${\bf C}$ code) to mainipulate R objects.

7.3 .Internal and .Primitive

The .Internal and .Primitive interfaces are used to call ${\bf C}$ code compiled into R at build time. See section ".Internal and .Primitive" in *Writing R Extensions*.

8 Exception handling

The exception handling facilities in R are provided through two mechanisms. Functions such as stop or warning can be called directly or options such as "warn" can be used to control the handling of problems.

8.1 stop

A call to stop halts the evaluation of the current expression, prints the message argument and returns execution to top-level.

8.2 warning

The function warning takes a single argument that is a character string. The behaviour of a call to warning depends on the value of the option "warn". If "warn" is negative warnings are ignored. If it is zero, they are stored and printed after the top-level function has completed. If it is one, they are printed as they occur and if it is 2 (or larger) warnings are turned into errors.

If "warn" is zero (the default), a top-level variable last.warning is created and the messages associated with each call to warning are stored, sequentially, in this vector. If there are fewer than 10 warnings they are printed after the function has finished evaluating. If there are more than 10 then a message indicating how many warnings occurred is printed. In either case last.warning contains the vector of messages.

8.3 on.exit

A function can insert a call to on.exit at any point in the body of a function. The effect of a call to on.exit is to store the value of the body so that it will be executed when the function exits. This allows the function to change some system parameters and to ensure that they are reset to appropriate values when the function is finished. The on.exit is guaranteed to be executed when the function exits either directly or as the result of a warning.

An error in the evaluation of the on.exit code causes an immediate jump to top-level without further processing of the on.exit code.

on.exit takes a single argument which is an expression to be evaluated when the function is exited.

8.4 restart

A call to **restart** effectively makes the function a possible point of return if an error occurs during the evaluation of that function (or one of the functions it calls).

restart takes a single argument which is a logical variable. If the value of the logical is TRUE then a jump-point is established. If the value is FALSE then the jump-point is removed.

When a jump is executed the jump-point is removed.

When an error occurs and one or more jump points are active then control is returned to the innermost function that has a jump-point established. Execution begins with the first statement in the body of the selected function. The environment for subsequent evaluation is the environment that was in effect at the time that the error that triggered the jump was signalled.

8.5 Error options

There are a number of options variables that can be used to control how R handles errors and warnings. The are listed in the table below.

'warn' Controls the printing of warnings.

'warning.expression'

Sets an expression that is to be evaluated when a warning occurs. The normal printing of warnings is suppressed if this option is set.

'error' Installs an expression that will be evaluated when an error occurs. The normal printing of error messages and warning messages precedes the evaluation of the expression.

Expressions installed by options("error") are evaluated before calls to on.exit are carried out.

One can use options(error = expression(q("yes"))) to get R to quit when an error has been signalled. In this case an error will cause R and the environment will be saved.

9 Debugging

Debugging code has always been a bit of an art. R provides several tools that help users find problems in their code. These tools halt execution at particular points in the code and the current state of the computation can be inspected.

Most debugging takes place either through calls to browser or debug. Both of these functions rely on the same internal mechanism and both provide the user with a special prompt. Any command can be typed at the prompt. The evaluation environment for the command is the currently active environment. This allows you to examine the current state of any variables etc.

There are five special commands that R interprets differently. They are,

'(RET)' Go to the next statement if the function is being debugged. Continue execution if the browser was invoked.

'с'

'where'

'cont' Continue the execution.

'n' Execute the next statement in the function. This works from the browser as well.

Show the call stack

'Q' Halt execution and jump to the top-level immediately.

If there is a local variable with the same name as one of the special commands listed above then its value can be accessed by using get. A call to get with the name in quotes will retrieve the value in the current environment.

The debugger provides access only to interpreted expressions. If a function calls a foreign language (such as **C**) then no access to the statements in that language is provided. Execution will halt on the next statement that is evaluated in R. A symbolic debugger such as **gdb** can be used to debug compiled code.

9.1 browser

A call to the function browser causes R to halt execution at that point and to provide the user with a special prompt. Arguments to browser are ignored.

```
> foo <- function(s) {
+ c <- 3
+ browser()
+ }
> foo(4)
Called from: foo(4)
Browse[1]> s
[1] 4
Browse[1]> get("c")
[1] 3
Browse[1]>
```

9.2 debug/undebug

The debugger can be invoked on any function by using the command debug(fun). Subsequently, each time that function is evaluated the debugger is invoked. The debugger allows you to control the evaluation of the statements in the body of the function. Before each statement is executed the statement is printed out and a special prompt provided. Any command can be given, those in the table above have special meaning.

Debugging is turned off by a call to undebug with the function as an argument.

```
> debug(mean.default)
> mean(1:10)
debugging in: mean.default(1:10)
debug: {
    if (na.rm)
        x \leftarrow x[!is.na(x)]
    trim <- trim[1]</pre>
    n <- length(c(x, recursive = TRUE))</pre>
    if (trim > 0) {
         if (trim >= 0.5)
             return(median(x, na.rm = FALSE))
         lo <- floor(n * trim) + 1</pre>
        hi <- n + 1 - lo
        x <- sort(x, partial = unique(c(lo, hi)))[lo:hi]
        n <- hi - lo + 1
    }
    sum(x)/n
}
Browse[1]>
debug: if (na.rm) x \leftarrow x[!is.na(x)]
Browse[1]>
debug: trim <- trim[1]
Browse[1]>
debug: n <- length(c(x, recursive = TRUE))</pre>
Browse[1] > c
exiting from: mean.default(1:10)
[1] 5.5
```

9.3 trace/untrace

Another way of monitoring the behaviour of R is through the trace mechanism. trace is called with a single argument that is the name of the function you want to trace. The name does not need to be quoted but for some functions you will need to quote the name in order to avoid a syntax error.

When trace has been invoked on a function then every time that function is evaluated the call to it is printed out. This mechanism is removed by calling untrace with the function as an argument.

```
> get("[<-")
.Primitive("[<-")
> trace("[<-")</pre>
```

```
> x <- 1:10
> x[3] <- 4
trace: "[<-"(*tmp*, 3, value = 4)
```

9.4 traceback

When an error has caused a jump to top-level a special variable called .Traceback is placed into the top-level workspace. .Traceback is a character vector with one entry for each function call that was active at the time the error occurred. An examination of .Traceback can be carried out by a call to traceback.

10 Parser

The parser is what converts the textual representation of R code into an internal form which may then be passed to the R evaluator which causes the specified instructions to be carried out. The internal form is itself an R object and can be saved and otherwise manipulated within the R system.

10.1 The parsing process

10.1.1 Modes of parsing

Parsing in R occurs in three different variants:

- The read-eval-print loop
- Parsing of text files
- Parsing of character strings

The read-eval-print loop forms the basic command line interface to R. Textual input is read until a complete R expression is available. Expressions may be split over several input lines. The primary prompt (by default '> ') indicates that the parser is ready for a new expression, and a continuation prompt (by default '+ ') indicates that the parser expects the remainder of an incomplete expression. The expression is converted to internal form during input and the parsed expression is passed to the evaluator and the result is printed (unless specifically made invisible). If the parser finds itself in a state which is incompatible with the language syntax, a "Syntax Error" is flagged and the parser resets itself and resumes input at the beginning of the next input line.

Text files can be parsed using the parse function. In particular, this is done during execution of the source function, which allows commands to be stored in an external file and executed as if they had been typed at the keyboard. Note, though, that the entire file is parsed and syntax checked before any evaluation takes place.

Character strings, or vectors thereof, can be parsed using the text= argument to parse. The strings are treated exactly as if they were the lines of an input file.

10.1.2 Internal representation

Parsed expressions are stored in an R object containing the parse tree. A fuller description of such objects can be found in Section 2.1.3 [Language objects], page 3 and Section 2.1.4 [Expression objects], page 4. Briefly, every elementary R expression is stored in function call form, as a list with the first element containing the function name and the remainder containing the arguments, which may in turn be further R expressions. The list elements can be named, corresponding to tagged matching of formal and actual arguments. Note that all R syntax elements are treated in this way, e.g. the assignment x <- 1 is encoded as "<-"(x, 1).

10.1.3 Deparsing

Any R object can be converted to an R expression using deparse. This is frequently used in connection with output of results, e.g. for labeling plots. Notice that only objects of mode "expression" can be expected to be unchanged by reparsing the output of deparsing. For instance, the numeric vector 1:5 will deparse as "c(1, 2, 3, 4, 5)", which will reparse as a call to the function c. As far as possible, evaluating the deparsed and reparsed expression gives the same result as evaluating the original, but there are a couple of awkward exceptions, mostly involving expressions that weren't generated from a textual representation in the first place.

10.2 Tokens

Tokens are the elementary building blocks of a programming language. They are recognised during *lexical analysis* which (conceptually, at least) takes place prior to the syntactic analysis performed by the parser itself.

10.2.1 Constants

There are four types of constants, logical, numeric, complex and string.

In addition, there are four special constants, NULL, NA, Inf, and NaN.

NULL is used to indicate the empty object. NA is used for absent ("Not Available") data values. Inf denotes infinity and NaN is not-a-number in the IEEE floating point calculus (results of the operations respectively 1/0 and 0/0, for instance).

Logical constants are either TRUE or FALSE.

Numeric constants follow a similar syntax to that of the C language. They consist of an integer part consisting of zero or more digits, followed optionally by '.' and a fractional part of zero or more digits optionally followed by an exponent part consisting of an 'E' or an 'e', an optional sign and a string of zero or more digits. Either the fractional or the decimal part can be empty, but not both at once.

Valid numeric constants: 1 10 0.1 .2 1e-7 1.2e+7 2e 3e+

The two latter examples are hardly useful in practice, but they are accepted and treated as '2' and '3', respectively.

Notice that there is no separate class of integer constants.

Note also that a preceding sign is treated as a unary operator, not as part of the constant.

Complex constants have the form of a numeric constant followed by 'i'. Notice that only purely imaginary numbers are actual constants, other complex numbers are parsed a unary or binary operations on numeric and imaginary numbers.

Valid complex constants: 2i 4.1i 1e-2i

String constants are delimited by a pair of single (''') or double ("') quotes and can contain all other printable characters. Quotes and other special characters within strings are specified using *escape sequences*:

\' single quote

\" double quote

\n newline

\t tab character

\b backspace

\nnn character with given code

A single quote may also be embedded directly in a double-quote delimited string and vice versa. The string "NA" has special meaning as the "missing string".

10.2.2 Identifiers

Identifiers consist of a sequence of letters, digits and the period symbol ('.'). They must not start with a digit, nor with a period followed by a digit.

The definition of a letter depends on the current locale. If this is configured correctly (this is system-dependent) one can use native language characters in identifiers.

Notice that identifiers starting with a period are not by default listed by the ls function and that '...' and '..1', '..2', etc. are special.

Notice also that objects can have names that are not identifiers. These are generally accessed via get and assign, although they can also be represented by text strings in some limited circumstances when there is no ambiguity (e.g. "x" <- 1). As get and assign are not restricted to names that are identifiers they do not recognise subscripting operators or assignment functions. The following pairs are *not* equivalent

```
x$a<-1     assign("x$a",1)
x[[1]]     get("x[[1]]")
names(x)<-nm     assign("names(x)",nm)</pre>
```

10.2.3 Reserved words

The following identifiers have a special meaning and should not be used for object names

```
if else repeat while function for in next break TRUE FALSE NULL NA Inf NaN \dots 1 \dots 2 etc.
```

10.2.4 Special operators

R allows user-defined infix operators. These have the form of a string of characters delimited by the '%' character. The string can contain any printable symbol except '%'. The escape sequences for strings do not apply here.

Note that the following operators are predefined

```
%% %*% %/% %in% %o% %x%
```

10.2.5 Separators

Although not strictly tokens, stretches of whitespace characters (spaces and tabs) serve to delimit tokens in case of ambiguity, (compare x<-5 and x<-5).

Semicolons (';') are used to separate elementary expressions.

Newlines have a function which is a combination of token separator and expression terminator. If an expression can terminate at the end of the line the parser will assume it does so, otherwise the newline is treated as whitespace.

Special rules apply to the else keyword: inside a compound expression, a newline before else is discarded, whereas at the outermost level, the newline terminates the if construction and a subsequent else causes a syntax error. This somewhat anomalous behaviour occurs because R should be usable in interactive mode and then it must decide whether the input expression is complete, incomplete, or invalid as soon as the user presses $\langle \overline{\text{RET}} \rangle$.

The comma (',') is used to separate function arguments and multiple indices.

10.2.6 Operator tokens

R uses the following operator tokens

(Several of the operators have different meaning inside model formulas)

10.2.7 Grouping symbols

Ordinary parentheses—'(' and ')'—are used for explicit grouping within expressions and to delimit the argument lists for function definitions and function calls.

Braces—'{' and '}'—delimit blocks of expressions in function definitions, conditional expressions, and iterative constructs.

10.2.8 Indexing tokens

Indexing of arrays and vectors performed using the single and double bracket symbols, '[]' and '[[]]'. Also, indexing tagged lists may be done using the '\$' operator.

10.3 Expressions

An R program consists of a sequence of R expressions. An expression can be a simple expression consisting of only a constant or an identifier, or it can be a compound expression constructed from other parts (which may themselves be expressions).

The following sections detail the various syntactical constructs that are available.

10.3.1 Function calls

A function call takes the form of a function reference followed by a comma-separated list of arguments within a set of parentheses.

```
function_reference ( arg1, arg2, ....., argn )
```

The function reference can be either

- an identifier (the name of the function)
- a text string (ditto, but handy if the function has a name which is not a valid identifier)
- an expression (which should evaluate to a function object)

Each argument can be tagged (tag=expr), or just be a simple expression. It can also be empty or it can be one of the special symbols '...', '...2', etc.

A tag can be an identifier or a text string.

Examples:

```
f(x)
g(tag = value, , 5)
"odd name"("strange tag" = 5, y)
(function(x) x^2)(5)
```

10.3.2 Infix and prefix operators

The order of precedence (highest first) of the operators are

```
- + (unary)
:
%xyz%
* / %%
+ - (binary)
> >= < <= == !=
!
&
|
""" (unary and binary)
-> <-
```

The exponentiation operator ' $^{^{\circ}}$ ' and the left assignment operator ' $^{^{\circ}}$ ' group right to left, all other operators group left to right. That is, 2 $^{^{\circ}}$ 2 $^{^{\circ}}$ 3 is 2 $^{^{\circ}}$ 8, not 4 $^{^{\circ}}$ 3, whereas 1 - 1 - 1 is -1, not 1.

Although it is not strictly an operator, it also needs mentioning that the '=' symbol is used for tagging arguments in function calls and for assigning default values in function definitions.

The '\$' symbol is in some sense an operator, but does not allow arbitrary right hand sides and is discussed under Section 10.3.3 [Index constructions], page 52. It has higher precedence than any of the other operators.

The parsed form of a unary or binary operation is completely equivalent to a function call with the operator symbol as the function name and the operands as the function arguments.

Parentheses are recorded as equivalent to a unary operator, with name "(", even in cases where the parentheses could be inferred from operator precedence (e.g., a * (b + c)).

Notice that the assignment symbols are operators just like the arithmetic, relational, and logical ones. Any expressions is allowed also on the target side of an assignment, as far as the parser is concerned (2 + 2 < -5) is a valid expression as far as the parser is concerned. The evaluator will object, though). Similar comments apply to the model formula operator.

52

10.3.3 Index constructions

R has three indexing constructs, two of which are syntactically similar although with somewhat different semantics:

```
object [ arg1, ....., argn ] object [[ arg1, ....., argn ]]
```

The *object* can formally be any valid expression, but it is understood to denote or evaluate to a subsetable object. The arguments generally evaluate to numerical or character indices, but other kinds of arguments are possible (notably drop = FALSE).

Internally, these index constructs are stored as function calls with function name "[" respectively "[[".

The third index construction is

```
object $ tag
```

Here, object is as above, whereas tag is an identifier or a text string. Internally, it is stored as a function call with name "\$"

10.3.4 Compound expressions

A compound expression is of the form

```
{ expr1 ; expr2 ; \dots ; exprn }
```

The semicolons may be replaced by newlines. Internally, this is stored as a function call with "{" as the function name and the expressions as arguments.

10.3.5 Flow control elements

R contains the following control structures as special syntactic constructs

```
if ( cond ) expr
if ( cond ) expr1 else expr2
while ( cond ) expr
repeat expr
for ( var in list ) expr
```

The expressions in these constructs will typically be compound expressions.

Within the loop constructs (while, repeat, for), one may use break (to terminate the loop) and next (to skip to the next iteration).

Internally, the constructs are stored as function calls:

```
"if"(cond, expr)
"if"(cond, expr1, expr2)
"while"(cond, expr)
"repeat"(expr)
"for"(var, list, expr)
"break"()
"next"()
```

10.3.6 Function definitions

A function definition is of the form

function (arglist) body

The function body is an expression, often a compound expression. The *arglist* is a comma-separated list of items each of which can be an identifier, or of the form '*identifier* = *default*', or the special symbol '...'. The *default* can be any valid expression.

Notice that function arguments unlike list tags, etc., cannot have "strange names" given as text strings.

Internally, a function definition is stored as a function call with function name function and two arguments, the *arglist* and the *body*. The *arglist* is stored as a tagged pairlist where the tags are the argument names and the values are the default expressions.

Function and Variable Index

\$	\mathbf{F}
\$	file.access 40 file.append 40 file.choose 40 file.copy 40
.C 40 .Call 40 .External 40 .Fortran 40 .Internal 41 .Primitive 41	file.create 40 file.exists 40 file.info 40 file.path 40 file.remove 40 file.show 40 for 14 formals 4, 39 formals 39
[G get
A	ī
as.call	is.na
as.name	\mathbf{M}
assign 49 attr 6 attr<-	match.arg 23 match.call 23, 38 match.fun 23 missing 15 mode 2
В	${f N}$
basename 40 body 4, 39 body 39 break 13 browser 44	NA 15, 17 names 7 names<
D	NextMethod 30 NULL 5
debug. 45 dirname. 40 do.call. 39	O on.exit
E	P
environment 4, 39 environment 39 eval 36	pairlist

${f Q}$ quote	Sys.timezone 40 system 40 system.time 40
\mathbf{R}	${f T}$
repeat	trace
restart	traceback
	$\verb typeof$
\mathbf{S}	
stop	\mathbf{U}
stop	Č
•	U undebug
storage.mode	undebug
storage.mode 2 substitute 34	undebug
storage.mode 2 substitute 34 switch 14	undebug. 45 unlink. 40 untrace. 45
storage.mode 2 substitute 34 switch 14 Sys.getenv 40	undebug. 45 unlink. 40 untrace. 45 UseMethod. 28
storage.mode 2 substitute 34 switch 14 Sys.getenv 40 Sys.getlocale 40	undebug. 45 unlink. 40 untrace. 45
storage.mode 2 substitute 34 switch 14 Sys.getenv 40 Sys.getlocale 40 Sys.localeconv 40	undebug. 45 unlink. 40 untrace. 45 UseMethod. 28

Appendix A References

Richard A. Becker, John M. Chambers and Allan R. Wilks (1988), *The New S Language*. Chapman & Hall, New York. This book is often called the " $Blue\ Book$ ".