

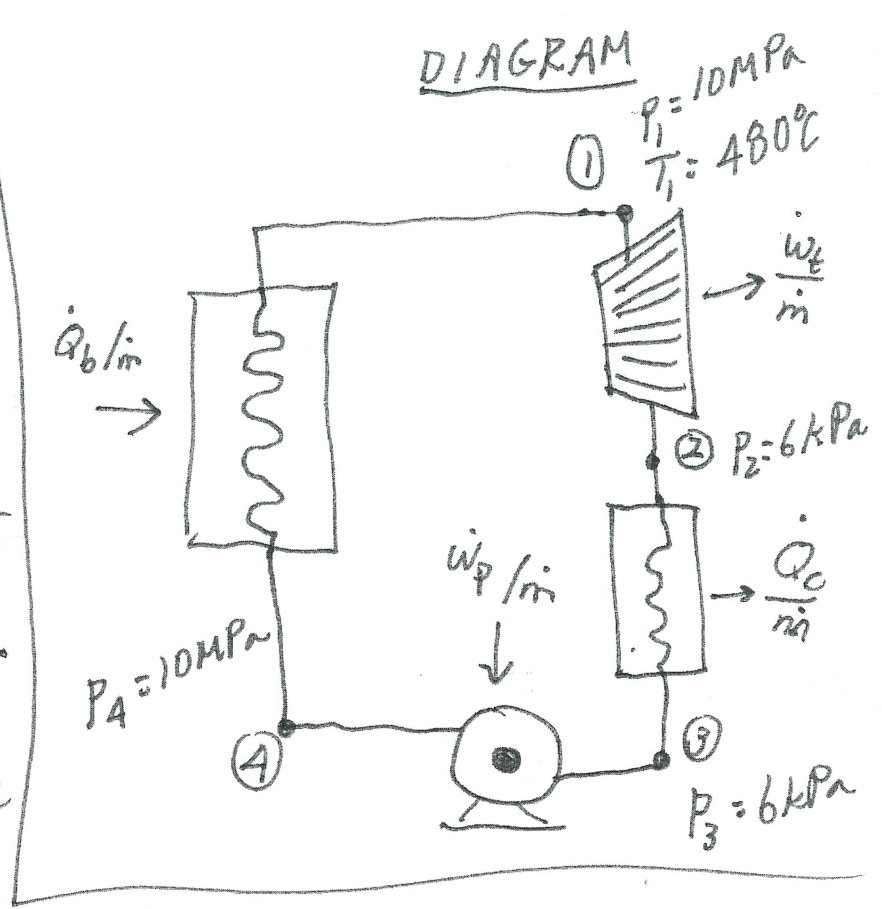
M.S. 8.2

GIVEN: Ideal Rankine cycle
 P_1, T_1, P_2, P_3, P_4

FIND: (a) \dot{Q}_b / \dot{m}
(b) η
(c) \dot{Q}_c / \dot{m}

ASSUME: Usual assumptions for an ideal Rankine cycle:

- $\Delta p = 0$ in boiler/condenser.
- Adiabatic pump/turbine.
- KES & PE effects are negligible
- Reversible processes; $\dot{\sigma} = 0$



These assumptions imply isentropic turbines/compressors.

Also: $\frac{\dot{Q}}{\dot{m}} = \Delta h$ for boiler/condenser.

$\frac{\dot{W}}{\dot{m}} = \Delta h$ for turbine/pump.

ANALYSIS: To get (a)-(c), we need $h_1 \rightarrow h_4$. Let's get these.

① Superheated table gives $h_1 = 3321.4 \text{ kJ/kg}$. I know I'll need entropy for state ②, so $s_1 = 6.5282 \text{ kJ/kg}\cdot\text{K}$

State ② $P_2 = 6 \text{ kPa}$ $s_2 = s_1 = 6.5282 \text{ kJ/kg}\cdot\text{K}$

This is a saturated state: $s_2 = 6.5282 = (1-x)s_f + x s_g$

This gives $x_2 = 0.7692$ which gives

$h_2 = 2009.8 \text{ kJ/kg}$

M.S. 8.2 cont'd

state ③ At this point we need to make one more assumption since all we have at states ③ & ④ are pressure. The typical assumption at this point is to assume state ③ is saturated liquid.

From saturated table:

$$h_3 = h_f(0.06 \text{ bar}) = 151.53 \frac{\text{kJ}}{\text{kg}}$$

$$s_3 = 0.5210 \text{ kJ/kg}\cdot\text{K}$$

state ④ $s_4 = s_3 = 0.5210 \text{ kJ/kg}\cdot\text{K}$

$$P_4 = 10 \text{ MPa}$$

Interpolating for h in the subcooled tables gives:

$$h_4 = 161.96 \text{ kJ/kg}$$

Now solve for (a), (b), (c)

$$(a) \quad \dot{Q}_b / \dot{m} = h_1 - h_4 = 3159.4 \text{ kJ/kg}$$

$$(b) \quad \eta = \frac{\dot{W}_t / \dot{m} - \dot{W}_p / \dot{m}}{\dot{Q}_b / \dot{m}} = \frac{(h_1 - h_2) - (h_4 - h_3)}{h_1 - h_4} = 0.412$$

$$(c) \quad \dot{Q}_c / \dot{m} = h_2 - h_3 = 1858.3 \text{ kJ/kg}$$