

Formulas

$$P(F_j|E) = \frac{P(EF_j)}{P(E)} = \frac{P(F_j)P(E|F_j)}{\sum_i P(F_i)P(E|F_i)}$$

Bernoulli(p): $E(X) = p$, $\text{Var}(X) = p(1-p)$, $\phi(t) = (1-p) + pe^t$

Binomial(n, p): $E(X) = np$, $\text{Var}(X) = np(1-p)$, $\phi(t) = [(1-p) + pe^t]^n$

Geometric(p): $E(X) = \frac{1}{p}$, $\text{Var}(X) = \frac{1-p}{p^2}$, $\phi(t) = \frac{pe^t}{1 - (1-p)e^t}$

Poisson(λ): $E(X) = \lambda$, $\text{Var}(X) = \lambda$, $\phi(t) = e^{\lambda(e^t-1)}$

Exponential(λ): $E(X) = \frac{1}{\lambda}$, $\text{Var}(X) = \frac{1}{\lambda^2}$, $\phi(t) = \frac{\lambda}{\lambda - t}$

$$\text{var}(X) = E(X^2) - [E(X)]^2$$

$$\text{cov}(X, Y) = E(XY) - E(X)E(Y)$$

$$\text{var}(X + Y) = \text{var}(X) + \text{var}(Y) + 2 \text{cov}(X, Y)$$

Gambler's Ruin: $y_i = \frac{1 - r^i}{1 - r^N}$ if $r \neq 1$; $y_i = \frac{i}{N}$ if $r = 1$

$$P\{S_n^A < S_m^B\} = \sum_{i=0}^{m-1} \binom{n+m-1}{n+i} p^{n+i} (1-p)^{m-1-i}$$